

9.4 Day Two

$$Y = A \sin(B(x - C)) + D$$

↑ ↑ ↑ ↑
 CONTROLS CONTROLS CONTROLS CONTROLS
 Amplitude PERIOD LEFT/RIGHT UP/DOWN
 VERTICAL HORIZONTAL HORIZONTAL VERTICAL
 STRETCH STRETCH SHIFT SHIFT

OF THE FOUR TRANSLATIONS OF THE SINE AND COSINE GRAPHS, WE ARE ONLY WORKING WITH A & B FOR NOW

Stretching and Shrinking Sine and Cosine Functions

The graphs of $y = a \sin bx$ and $y = a \cos bx$ represent transformations of their parent functions. The value of a indicates a vertical stretch ($a > 1$) or a vertical shrink ($0 < a < 1$) and changes the amplitude of the graph. The value of b indicates a horizontal stretch ($0 < b < 1$) or a horizontal shrink ($b > 1$) and changes the period of the graph.

$$y = a \sin bx$$

$$y = a \cos bx$$

vertical stretch or shrink by a factor of a horizontal stretch or shrink by a factor of $\frac{1}{b}$

$$\text{PERIOD} = \frac{2\pi}{b}$$

$$b = \frac{2\pi}{\text{PERIOD}}$$

Core Concept

Amplitude and Period

The amplitude and period of the graphs of $y = a \sin bx$ and $y = a \cos bx$, where a and b are nonzero real numbers, are as follows:

$$\text{Amplitude} = |a|$$

$$\text{Period} = \frac{2\pi}{|b|}$$

$$\left. \begin{aligned} y &= -\sin(x) \\ y &= -\cos(x) \end{aligned} \right\}$$

A NEGATIVE "A" VALUE CREATES A REFLECTION ABOUT THE CENTER LINE AXIS

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