Big Ideas

- **Reinforcement of Algebra 1 Standard 6.0** Students graph a linear equation and compute the \(x\)- and \(y\)-intercepts (e.g., graph \(2x + 6y = 4\)). They are also able to sketch the region defined by linear inequality (e.g., they sketch the region defined by \(2x + 6y < 4\)). (Key)

- **Reinforcement of Algebra 1 Standard 7.0** Students verify that a point lies on a line, given an equation of the line. Students are able to derive linear equations by using the point-slope formula. (Key)

**Key Vocabulary**
- dependent variable (p. 61)
- domain (p. 58)
- function (p. 58)
- independent variable (p. 61)
- relation (p. 58)

Real-World Link

Underground Temperature Linear equations can be used to model relationships between many real-world quantities. The equations can then be used to make predictions such as the temperature of underground rocks.

Foldables Study Organizer

1. **Fold** in half along the width and staple along the fold.

2. **Turn** the fold to the left and write the title of the chapter on the front. On each left-hand page of the booklet, write the title of a lesson from the chapter.

Linear Relations and Functions Make this Foldable to help you organize your notes. Begin with four sheets of grid paper.
GET READY for Chapter 2

Diagnose Readiness  You have two options for checking Prerequisite Skills.

Option 1

Take the Quick Check below. Refer to the Quick Review for help.

Write the ordered pair for each point.  (Prerequisite Skill)


Example 1  Write the ordered pair for point G.

Step 1  Follow a vertical line through the point to find the x-coordinate on the x-axis. The x-coordinate is 7.

Step 2  Follow a horizontal line through the point to find the y-coordinate on the y-axis. The y-coordinate is −5.

Step 3  The ordered pair for point G is (7, −5). It can also be written as G(7, −5).

Evaluate each expression if $a = −1$, $b = 3$, $c = −2$, and $d = 0$.  (Prerequisite Skill)

9. $c + d$  10. $4c − b$  11. $a^2 − 5a + 3$  12. $2b^2 + b + 7$  13. $\frac{a − b}{c − d}$  14. $\frac{a + c}{b + c}$

Simplify each expression.  (Prerequisite Skill)

15. $x − (−1)$  16. $x − (−5)$  17. $2[x − (−3)]$  18. $4[x − (−2)]$

Example 2  Evaluate $d(a^2 + 2ab + b^2) − c$ if $a = −1$, $b = 3$, $c = −2$, and $d = 0$.

$0[(-1)^2 + 2(−1)(3) + 3^2] − (−2)$  Substitute $−1$ for $a$, $3$ for $b$, $−2$ for $c$, and $0$ for $d$.

$0 − (−2)$  Multiplication Property of Zero.

$= 2$  Subtract.

Example 3  Simplify $\frac{2}{5}[x − (−10)]$.

$\frac{2}{5}[x − (−10)]$  Simplify.

$= \frac{2}{5}(x + 10)$

$= \frac{2}{5}(x) + \frac{2}{5}(10)$  Distributive Property

$= \frac{2}{5}x + 4$  Simplify.

Example 2  Evaluate $d(a^2 + 2ab + b^2) − c$ if $a = −1$, $b = 3$, $c = −2$, and $d = 0$.

$0[(-1)^2 + 2(−1)(3) + 3^2] − (−2)$  Substitute $−1$ for $a$, $3$ for $b$, $−2$ for $c$, and $0$ for $d$.

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$= \frac{2}{5}(x + 10)$

$= \frac{2}{5}(x) + \frac{2}{5}(10)$  Distributive Property

$= \frac{2}{5}x + 4$  Simplify.

ANIMALS  A blue whale’s heart beats 9 times a minute.

7. Make a table of ordered pairs in which the x-coordinate represents the number of minutes and the y-coordinate represents the number of heartbeats.  (Prerequisite Skill)

8. Graph the ordered pairs.  (Prerequisite Skill)

19. TRAVEL  Joan travels 65 miles per hour for $x$ hours on Monday. On Tuesday she drives 55 miles per hour for $(x + 3)$ hours. Write a simplified expression for the sum of the distances traveled.  (Prerequisite Skill)
The table shows average and maximum lifetimes for some animals. The data can also be represented as the ordered pairs \((12, 28), (15, 30), (8, 20), (12, 20),\) and \((20, 50)\). The first number in each ordered pair is the average lifetime, and the second number is the maximum lifetime.

\[
\text{Animal} \quad \text{Average Lifetime (years)} \quad \text{Maximum Lifetime (years)}
\]

<table>
<thead>
<tr>
<th>Animal</th>
<th>Average Lifetime</th>
<th>Maximum Lifetime</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cat</td>
<td>12</td>
<td>28</td>
</tr>
<tr>
<td>Cow</td>
<td>15</td>
<td>30</td>
</tr>
<tr>
<td>Deer</td>
<td>8</td>
<td>20</td>
</tr>
<tr>
<td>Dog</td>
<td>12</td>
<td>20</td>
</tr>
<tr>
<td>Horse</td>
<td>20</td>
<td>50</td>
</tr>
</tbody>
</table>

Source: The World Almanac

**Graph Relations** You can graph the ordered pairs above on a coordinate system. Remember that each point in the coordinate plane can be named by exactly one ordered pair and every ordered pair names exactly one point in the coordinate plane.

The graph of the animal lifetime data lies in the part of the Cartesian coordinate plane with all positive coordinates. The **Cartesian coordinate plane** is composed of the \(x\)-axis (horizontal) and the \(y\)-axis (vertical), which meet at the origin \((0, 0)\) and divide the plane into four quadrants. In general, any ordered pair in the coordinate plane can be written in the form \((x, y)\).

A **relation** is a set of ordered pairs, such as the one for the longevity of animals. The **domain** of a relation is the set of all first coordinates \((x\)-coordinates) from the ordered pairs, and the **range** is the set of all second coordinates \((y\)-coordinates) from the ordered pairs. The domain of the function above is \(\{8, 12, 15, 20\}\), and the range is \(\{20, 30, 28, 50\}\).

A **function** is a special type of relation in which each element of the domain is paired with exactly one element of the range. A **mapping** shows how the members are paired. A function like the one represented by the mapping in which each element of the range is paired with exactly one element of the domain is called a **one-to-one function**.
If no vertical line intersects a graph in more than one point, the graph represents a function. If some vertical line intersects a graph in two or more points, the graph does not represent a function.

In Example 1, there is no vertical line that contains more than one of the points. Therefore, the relation is a function.
**EXAMPLE**  Vertical Line Test

**GEOGRAPHY** The table shows the population of the state of California over the last several decades. Graph this information and determine whether it represents a function. Is the relation discrete or continuous?

<table>
<thead>
<tr>
<th>Year</th>
<th>Population (millions)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1950</td>
<td>10.6</td>
</tr>
<tr>
<td>1960</td>
<td>15.7</td>
</tr>
<tr>
<td>1970</td>
<td>19.9</td>
</tr>
<tr>
<td>1980</td>
<td>23.7</td>
</tr>
<tr>
<td>1990</td>
<td>29.8</td>
</tr>
<tr>
<td>2000</td>
<td>33.9</td>
</tr>
</tbody>
</table>

*Source: U.S. Census Bureau*

Use the vertical line test. Notice that no vertical line can be drawn that contains more than one of the data points. Therefore, this relation is a function. Because the graph consists of distinct points, the relation is discrete.

**Example**

2. The number of employees a company had in each year from 1999 to 2004 were 25, 28, 34, 31, 27, and 29. Graph this information and determine whether it represents a function. Is the relation discrete or continuous?

**Equations of Functions and Relations** Relations and functions can also be represented by equations. The solutions of an equation in x and y are the set of ordered pairs (x, y) that make the equation true.

Consider the equation \( y = 2x - 6 \). Since \( x \) can be any real number, the domain has an infinite number of elements. To determine whether an equation represents a function, it is often simplest to look at the graph of the relation.

**EXAMPLE**

Graph a Relation

Graph each equation and find the domain and range. Then determine whether the equation is a function and state whether it is discrete or continuous.

a. \( y = 2x + 1 \)

Make a table of values to find ordered pairs that satisfy the equation. Choose values for \( x \) and find the corresponding values for \( y \). Then graph the ordered pairs.

Since \( x \) can be any real number, there is an infinite number of ordered pairs that can be graphed. All of them lie on the line shown. Notice that every real number is the \( x \)-coordinate of some point on the line. Also, every real number is the \( y \)-coordinate of some point on the line. So the domain and range are both all real numbers, and the relation is continuous.

This graph passes the vertical line test. For each \( x \)-value, there is exactly one \( y \)-value, so the equation \( y = 2x + 1 \) represents a function.
b. $x = y^2 - 2$

Make a table. In this case, it is easier to choose $y$ values and then find the corresponding values for $x$. Then sketch the graph, connecting the points with a smooth curve.

Every real number is the $y$-coordinate of some point on the graph, so the range is all real numbers. But, only real numbers greater than or equal to $-2$ are $x$-coordinates of points on the graph. So the domain is $\{x | x \geq -2\}$. The relation is continuous.

You can see from the table and the vertical line test that there are two $y$ values for each $x$ value except $x = -2$. Therefore, the equation $x = y^2 - 2$ does not represent a function.

3A. Graph the relation represented by $y = x^2 + 1$.
3B. Find the domain and range. Determine if the relation is discrete or continuous.
3C. Determine whether the relation is a function.

When an equation represents a function, the variable, usually $x$, whose values make up the domain is called the independent variable. The other variable, usually $y$, is called the dependent variable because its values depend on $x$.

Equations that represent functions are often written in function notation. The equation $y = 2x + 1$ can be written as $f(x) = 2x + 1$. The symbol $f(x)$ replaces the $y$ and is read “$f$ of $x$.” The $f$ is just the name of the function. It is not a variable that is multiplied by $x$. Suppose you want to find the value in the range that corresponds to the element 4 in the domain of the function. This is written as $f(4)$ and is read “$f$ of 4.” The value $f(4)$ is found by substituting 4 for each $x$ in the equation. Therefore, $f(4) = 2(4) + 1$ or 9. Letters other than $f$ can be used to represent a function. For example, $g(x) = 2x + 1$.

**EXAMPLE** Evaluate a Function

Given $f(x) = x^2 + 2$, find each value.

a. $f(-3)$

\[
\begin{align*}
  f(x) & = x^2 + 2 & \text{Original function} \\
  f(-3) & = (-3)^2 + 2 & \text{Substitute.} \\
  & = 9 + 2 & \text{Simplify.} \\
  & = 11 \\
\end{align*}
\]

b. $f(3z)$

\[
\begin{align*}
  f(x) & = x^2 + 2 & \text{Original function} \\
  f(3z) & = (3z)^2 + 2 & \text{Substitute.} \\
  & = 9z^2 + 2 & (ab)^2 = a^2b^2 \\
\end{align*}
\]

Given $g(x) = 0.5x^2 - 5x + 3.5$, find each value.

4A. $g(2.8)$

4B. $g(4a)$
State the domain and range of each relation. Then determine whether each relation is a function. Write yes or no.

1. D  
   3  
   2  
   1  
   0  
   2  

2. | x | y |
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>10</td>
<td>-2</td>
</tr>
<tr>
<td>15</td>
<td>-2</td>
</tr>
<tr>
<td>20</td>
<td>-2</td>
</tr>
</tbody>
</table>

3. (0, 1), (1, 2), (2, 3), (3, 4), (4, 5)

WEATHER For Exercises 4–6, use the table that shows the record high temperatures (°F) for January and July for four states.

4. Identify the domain and range. Assume that the January temperatures are the domain.
5. Write a relation of ordered pairs for the data.
6. Graph the relation. Is this relation a function?

Graph each relation or equation and find the domain and range. Then determine whether the relation or equation is a function and state whether it is discrete or continuous.

7. \{(7, 8), (7, 5), (7, 2), (7, -1)\}
8. \{(6, 2.5), (3, 2.5), (4, 2.5)\}

Example 4 (p. 61)

Graph each relation or equation and find the domain and range. Then determine whether the relation or equation is a function and state whether it is discrete or continuous.

9. \(y = -2x + 1\)
10. \(x = y^2\)

Example 4 (p. 61)

Determine whether each function is discrete or continuous.

11. Find \(f(5)\) if \(f(x) = x^2 - 3x\).
12. Find \(h(-2)\) if \(h(x) = x^3 + 1\).

State the domain and range of each relation. Then determine whether each relation is a function. Write yes or no.

13. D  
    20  
    10  
    30  

14. D  
    3  
    2  
    1  

15. | x | y |
    |---|---|
    | 0.5| -3 |
    | 2 | 0.8|
    | 0.5| 8 |

16. | x | y |
    |---|---|
    | 2000| 40000|
    | 2001| 43000|
    | 2002| 46000|
    | 2003| 45000|

17. Determine whether each function is discrete or continuous.

19. \(f(x)\)

20. \(f(x)\)

21. \{(-3, 0), (-1, 1), (1, 3)\}
22. \(y = -x + 4\)
Graph each relation or equation and find the domain and range. Then determine whether the relation or equation is a function and state whether it is discrete or continuous.

23. \[(2, 1), (-3, 0), (1, 5)\]  
24. \[(4, 5), (6, 5), (3, 5)\]

25. \[(-2, 5), (3, 7), (-2, 8)\]  
26. \[(3, 4), (4, 3), (6, 5), (5, 6)\]

27. \[(0, -1.1), (2, -3), (1.4, 2), (-3.6, 8)\]

28. \[(-2.5, 1), (-1, -1), (0, 1), (-1, 1)\]

29. \[y = -5x\]  
30. \[y = 3x\]  
31. \[y = 3x - 4\]  
32. \[y = 7x - 6\]  
33. \[y = x^2\]  
34. \[x = 2y^2 - 3\]

Find each value if \(f(x) = 3x - 5\) and \(g(x) = x^2 - x\).

35. \(f(-3)\)  
36. \(g(3)\)  
37. \(g\left(\frac{1}{3}\right)\)  
38. \(f\left(\frac{2}{3}\right)\)  
39. \(f(a)\)

40. \(g(5n)\)

41. Find the value of \(f(x) = -3x + 2\) when \(x = 2\).

42. What is \(g(4)\) if \(g(x) = x^2 - 5\)?

**SPORTS** For Exercises 43–45, use the table that shows the leading home run and runs batted in totals in the National League for 2000–2004.

<table>
<thead>
<tr>
<th>Year</th>
<th>HR</th>
<th>RBI</th>
</tr>
</thead>
<tbody>
<tr>
<td>2000</td>
<td>50</td>
<td>147</td>
</tr>
<tr>
<td>2001</td>
<td>73</td>
<td>160</td>
</tr>
<tr>
<td>2002</td>
<td>49</td>
<td>128</td>
</tr>
<tr>
<td>2003</td>
<td>47</td>
<td>141</td>
</tr>
<tr>
<td>2004</td>
<td>48</td>
<td>131</td>
</tr>
</tbody>
</table>

Source: The World Almanac

43. Make a graph of the data with home runs on the horizontal axis and runs batted in on the vertical axis.

44. Identify the domain and range.

45. Does the graph represent a function? Explain your reasoning.

**STOCKS** For Exercises 46–49, use the table that shows a company’s stock price in recent years.

<table>
<thead>
<tr>
<th>Year</th>
<th>Price</th>
</tr>
</thead>
<tbody>
<tr>
<td>2002</td>
<td>$39</td>
</tr>
<tr>
<td>2003</td>
<td>$43</td>
</tr>
<tr>
<td>2004</td>
<td>$48</td>
</tr>
<tr>
<td>2005</td>
<td>$55</td>
</tr>
<tr>
<td>2006</td>
<td>$61</td>
</tr>
<tr>
<td>2007</td>
<td>$52</td>
</tr>
</tbody>
</table>

46. Write a relation to represent the data.

47. Graph the relation.

48. Identify the domain and range.

49. Is the relation a function? Explain your reasoning.

**GOVERNMENT** For Exercises 50–53, use the table below that shows the number of members of the U.S. House of Representatives with 30 or more consecutive years of service in Congress from 1991 to 2003.

<table>
<thead>
<tr>
<th>Year</th>
<th>1991</th>
<th>1993</th>
<th>1995</th>
<th>1997</th>
<th>1999</th>
<th>2001</th>
<th>2003</th>
</tr>
</thead>
<tbody>
<tr>
<td>Representatives</td>
<td>11</td>
<td>12</td>
<td>9</td>
<td>6</td>
<td>3</td>
<td>7</td>
<td>9</td>
</tr>
</tbody>
</table>

Source: Congressional Directory

50. Write a relation to represent the data.

51. Graph the relation.

52. Identify the domain and range. Determine whether the relation is discrete or continuous.

53. Is the relation a function? Explain your reasoning.

54. **AUDIO BOOK DOWNLOADS** Chaz has a collection of 15 audio books. After he gets a part-time job, he decides to download 3 more audio books each month. The function \(A(t) = 15 + 3t\) counts the number of audio books \(A(t)\) he has after \(t\) months. How many audio books will he have after 8 months?
55. **H.O.T. Problems** Write a relation of four ordered pairs that is not a function. Explain why it is not a function.

56. **FIND THE ERROR** Teisha and Molly are finding \(g(2a)\) for the function \(g(x) = x^2 + x - 1\). Who is correct? Explain your reasoning.

\[
\begin{align*}
\text{Teisha} \\
g(2a) &= 2(a^2 + a - 1) \\
&= 2a^2 + 2a - 2
\end{align*}
\]

\[
\begin{align*}
\text{Molly} \\
g(2a) &= (2a)^2 + 2a - 1 \\
&= 4a^2 + 2a - 1
\end{align*}
\]

57. **CHALLENGE** If \(f(3a - 1) = 12a - 7\), find one possible expression for \(f(x)\).

58. **Writing in Math** Use the information about animal lifetimes on page 58 to explain how relations and functions apply to biology. Include an explanation of how a relation can be used to represent data and a sentence that includes the words *average lifetime*, *maximum lifetime*, and *function*.

59. **ACT/SAT** If \(g(x) = x^2\), which expression is equal to \(g(x + 1)\)?

A 1
B \(x^2 + 1\)
C \(x^2 + 2x + 1\)
D \(x^2 - x\)

60. **REVIEW** Which set of dimensions represent a triangle similar to the triangle shown below?

64. **SHOPPING** Javier had $25.04 when he went to the mall. His friend Sally had $32.67. Javier wanted to buy a shirt for $27.89. How much money did Javier borrow from Sally? How much money did that leave Sally? (Lesson 1-3)

51. **Simplify each expression.** (Lessons 1-1 and 1-2)

61. \(32(22 - 12) + 42\)
62. \(3(5a + 6b) + 8(2a - b)\)

52. **Solve each inequality.** (Lessons 1-5 and 1-6)

61. \(|y + 1| < 7\)
62. \(|5 - m| < 1\)
63. \(x - 5 < 0.1\)

53. **PREREQUISITE SKILL** Solve each equation. Check your solution. (Lesson 1-3)

67. \(x + 3 = 2\)
68. \(-4 + 2y = 0\)
69. \(0 = \frac{1}{2}x - 3\)
70. \(\frac{1}{3}x - 4 = 1\)
Discrete and Continuous Functions in the Real World

A cup of frozen yogurt costs $2 at the Yogurt Shack. We might describe the cost of \( x \) cups of yogurt using the continuous function \( y = 2x \), where \( y \) is the total cost in dollars. The graph of that function is shown at the right.

From the graph, you can see that 2 cups of yogurt cost $4, 3 cups cost $6, and so on. The graph also shows that 1.5 cups of yogurt cost \( 2(1.5) \) or $3. However, the Yogurt Shack probably will not sell partial cups of yogurt. This function is more accurately modeled with a discrete function.

The graph of the discrete function at the right also models the cost of buying cups of frozen yogurt. The domain in this graph makes sense in this situation.

When choosing a discrete function or a continuous function to model a real-world situation, be sure to consider whether all real numbers are reasonable as part of the domain.

Reading to Learn

Determine whether each function is better modeled using a discrete or continuous function. Explain your reasoning.

1. Converting Units

2. E-Mails Received

3. \( y \) represents the distance a car travels in \( x \) hours.

4. \( y \) represents the total number of riders who have ridden a roller coaster after \( x \) rides.

5. Give an example of a real-world function that is discrete and a real-world function that is continuous. Explain your reasoning.
Lolita has 4 hours after dinner to study and do homework. She has brought home math and chemistry. If she spends \( x \) hours on math and \( y \) hours on chemistry, a portion of the graph of the equation \( x + y = 4 \) can be used to relate how much time she spends on each.

**Identify Linear Equations and Functions**

An equation such as \( x + y = 4 \) is called a linear equation. A **linear equation** has no operations other than addition, subtraction, and multiplication of a variable by a constant. The variables may not be multiplied together or appear in a denominator. A linear equation does not contain variables with exponents other than 1. The graph of a linear equation is always a line.

### Linear equations

- \( 5x - 3y = 7 \)
- \( x = 9 \)
- \( 6s = -3t - 15 \)
- \( y = \frac{1}{2}x \)

### Not linear equations

- \( 7a + 4b^2 = -8 \)
- \( y = \sqrt{x} + 5 \)
- \( x + xy = 1 \)
- \( y = \frac{1}{x} \)

A **linear function** is a function whose ordered pairs satisfy a linear equation. Any linear function can be written in the form \( f(x) = mx + b \), where \( m \) and \( b \) are real numbers.

**EXAMPLE**

Identify Linear Functions

State whether each function is a linear function. Explain.

**a.** \( f(x) = 10 - 5x \)

This is a linear function because it can be written as \( f(x) = -5x + 10 \). \( m = -5, b = 10 \)

**b.** \( g(x) = x^4 - 5 \)

This is not a linear function because \( x \) has an exponent other than 1.

**c.** \( h(x, y) = 2xy \)

This is not a linear function because the two variables are multiplied together.

**1A.** \( f(x) = \frac{5}{x + 6} \)

**1B.** \( g(x) = -\frac{3}{2}x + \frac{1}{3} \)

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**Main Ideas**

- Identify linear equations and functions.
- Write linear equations in standard form and graph them.

**Reinforcement of Algebra I Standard 6.0**

Students graph a linear equation and compute the \( x \)- and \( y \)-intercepts (e.g., graph \( 2x + 6y = 4 \)). They are also able to sketch the region defined by linear inequality (e.g., they sketch the region defined by \( 2x + 6y < 4 \)). (Key, CAHSEE)

**New Vocabulary**

- linear equation
- linear function
- standard form
- \( y \)-intercept
- \( x \)-intercept

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**Main Ideas**

- Identify linear equations and functions.
- Write linear equations in standard form and graph them.

**Reinforcement of Algebra I Standard 6.0**

Students graph a linear equation and compute the \( x \)- and \( y \)-intercepts (e.g., graph \( 2x + 6y = 4 \)). They are also able to sketch the region defined by linear inequality (e.g., they sketch the region defined by \( 2x + 6y < 4 \)). (Key, CAHSEE)

**New Vocabulary**

- linear equation
- linear function
- standard form
- \( y \)-intercept
- \( x \)-intercept
**Real-World Example** Evaluate a Linear Function

**WATER PRESSURE** The linear function $P(d) = 62.5d + 2117$ can be used to find the pressure (lb/ft$^2$) $d$ feet below the surface of the water.

a. Find the pressure at a depth of 350 feet.

$$P(d) = 62.5d + 2117 \quad \text{Original function}$$

$$P(350) = 62.5(350) + 2117 \quad \text{Substitute.}$$

$$= 23,992 \quad \text{Simplify.}$$

The pressure at a depth of 350 feet is about 24,000 lb/ft$^2$.

b. The term 2117 in the function represents the atmospheric pressure at the surface of the water. How many times as great is the pressure at a depth of 350 feet as the pressure at the surface?

Divide the pressure 350 feet down by the pressure at the surface.

$$\frac{23,992}{2117} \approx 11.33 \quad \text{Use a calculator.}$$

The pressure at that depth is more than 11 times that at the surface.

2. At what depth is the pressure 33,367 lb/ft$^2$?

**Standard Form** Many linear equations can be written in **standard form**, $Ax + By = C$, where $A$, $B$, and $C$ are integers whose greatest common factor is 1.

**KEY CONCEPT**

**Standard Form of a Linear Equation**

The standard form of a linear equation is $Ax + By = C$, where $A$, $B$, and $C$ are integers whose greatest common factor is 1, $A \geq 0$, and $A$ and $B$ are not both zero.

**EXAMPLE** Standard Form

Write each equation in standard form. Identify $A$, $B$, and $C$.

a. $y = -2x + 3$

$$y = -2x + 3 \quad \text{Original equation}$$

$$2x + y = 3 \quad \text{Add } 2x \text{ to each side.}$$

So, $A = 2$, $B = 1$, and $C = 3$.

b. $-\frac{3}{5}x = 3y - 2$

$$-\frac{3}{5}x = 3y - 2 \quad \text{Original equation}$$

$$-\frac{3}{5}x - 3y = -2 \quad \text{Subtract } 3y \text{ from each side.}$$

$$3x + 15y = 10 \quad \text{Multiply each side by } -5 \text{ so that the coefficients are integers and } A \geq 0.$$ 

So, $A = 3$, $B = 15$, and $C = 10$.

**Extra Examples at** [ca.algebra2.com](http://ca.algebra2.com)
Since two points determine a line, one way to graph a linear equation or function is to find the points at which the graph intersects each axis and connect them with a line. The y-coordinate of the point at which a graph crosses the y-axis is called the y-intercept. Likewise, the x-coordinate of the point at which it crosses the x-axis is the x-intercept.

**EXAMPLE**  
**Use Intercepts to Graph a Line**

Find the x-intercept and the y-intercept of the graph of $3x - 4y + 12 = 0$. Then graph the equation.

The x-intercept is the value of $x$ when $y = 0$.

$3x - 4y + 12 = 0$ Original equation

$3x - 4(0) + 12 = 0$ Substitute 0 for $y$.

$3x = -12$ Subtract 12 from each side.

$x = -4$ Divide each side by 3.

The x-intercept is $-4$. The graph crosses the x-axis at $(-4, 0)$.

Likewise, the y-intercept is the value of $y$ when $x = 0$.

$3x - 4y + 12 = 0$ Original equation

$3(0) - 4y + 12 = 0$ Substitute 0 for $x$.

$-4y = -12$ Subtract 12 from each side.

$y = 3$ Divide each side by $-4$.

The y-intercept is 3. The graph crosses the y-axis at $(0, 3)$.

Use these ordered pairs to graph the equation.

4. Find the x-intercept and the y-intercept of the graph of $2x + 5y - 10 = 0$. Then graph the equation.

---

**Example 1**  
(p. 66)  
State whether each equation or function is linear. Write yes or no. If no, explain your reasoning.

1. $x^2 + y^2 = 4$
2. $h(x) = 1.1 - 2x$

**Example 2**  
(p. 67)  
**ECONOMICS**  
For Exercises 3 and 4, use the following information.

On January 1, 1999, the euro became legal tender in 11 participating countries in Europe. Based on the exchange rate on one particular day, the linear function $d(x) = 0.8881x$ could be used to convert x euros to U.S. dollars.

3. On that day, what was the value in U.S. dollars of 200 euros?
4. On that day, what was the value in euros of 500 U.S. dollars?

**Example 3**  
(p. 67)  
Write each equation in standard form. Identify $A$, $B$, and $C$.

5. $y = 3x - 5$
6. $4x = 10y + 6$
7. $y = \frac{2}{3}x + 1$

**Example 4**  
(p. 68)  
Find the x-intercept and the y-intercept of the graph of each equation. Then graph the equation.

8. $y = -3x - 5$
9. $x - y - 2 = 0$
State whether each equation or function is linear. Write yes or no. If no, explain your reasoning.

10. \( x + y = 5 \) \hspace{1cm} 11. \( f(x) = 6x - 19 \)
12. \( f(x) = 7x^5 + x - 1 \) \hspace{1cm} 13. \( h(x) = 2x^3 - 4x^2 + 5 \)
14. \( g(x) = 10 + \frac{2}{x^2} \) \hspace{1cm} 15. \( \frac{1}{x} + 3y = -5 \)
16. \( x + \sqrt{y} = 4 \) \hspace{1cm} 17. \( y = \sqrt{2x - 5} \)

**PHYSICS** For Exercises 18 and 19, use the following information.
When a sound travels through water, the distance \( y \) in meters that the sound travels in \( x \) seconds is given by the equation \( y = 1440x \).
18. How far does a sound travel underwater in 5 seconds?
19. In air, the equation is \( y = 343x \). Does sound travel faster in air or water? Explain.

**ATMOSPHERE** For Exercises 20 and 21, use the following information.
Suppose the temperature \( T \) in °F above the Earth’s surface is given by \( T(h) = -3.6h + 68 \), where \( h \) is the height (in thousands of feet).
20. Find the temperature at a height of 10,000 feet.
21. Find the height if the temperature is −58°F.

Write each equation in standard form. Identify \( A, B, \) and \( C \).

22. \( y = -3x + 4 \) \hspace{1cm} 23. \( y = 12x \) \hspace{1cm} 24. \( x = 4y - 5 \)
25. \( x = 7y + 2 \) \hspace{1cm} 26. \( 5y = 10x - 25 \) \hspace{1cm} 27. \( 4x = 8y - 12 \)

Find the \( x \)-intercept and the \( y \)-intercept of the graph of each equation. Then graph the equation.

28. \( 5x + 3y = 15 \) \hspace{1cm} 29. \( 2x - 6y = 12 \) \hspace{1cm} 30. \( 3x - 4y - 10 = 0 \)
31. \( 2x + 5y - 10 = 0 \) \hspace{1cm} 32. \( y = x \) \hspace{1cm} 33. \( y = 4x - 2 \)

**GEOMETRY** Find the area of the shaded region in the graph. (Hint: The area of a trapezoid is given by \( A = \frac{1}{2}h(b_1 + b_2) \).)

Write each equation in standard form. Identify \( A, B, \) and \( C \).

35. \( \frac{1}{2}x + \frac{1}{2}y = 6 \) \hspace{1cm} 36. \( \frac{1}{3}x - \frac{1}{3}y = -2 \) \hspace{1cm} 37. \( 0.5x = 3 \)
38. \( 0.25y = 10 \) \hspace{1cm} 39. \( \frac{5}{6}x + \frac{1}{15}y = \frac{3}{10} \) \hspace{1cm} 40. \( 0.25x = 0.1 + 0.2y \)

Find the \( x \)-intercept and the \( y \)-intercept of the graph of each equation. Then graph the equation.

41. \( y = -2 \) \hspace{1cm} 42. \( y = 4 \) \hspace{1cm} 43. \( x = 8 \) \hspace{1cm} 44. \( 3x + 2y = 6 \)
45. \( x = 1 \) \hspace{1cm} 46. \( f(x) = 4x - 1 \) \hspace{1cm} 47. \( g(x) = 0.5x - 3 \) \hspace{1cm} 48. \( 4x + 8y = 12 \)
49. **ATMOSPHERE** Graph the linear function in Exercises 20 and 21.
**Commission** For Exercises 50–52, use the following information.
Latonya earns a commission of $1.75 for each magazine subscription she sells and $1.50 for each newspaper subscription she sells. Her goal is to earn a total of $525 in commissions in the next two weeks.

50. Write an equation that is a model for the different numbers of magazine and newspaper subscriptions that can be sold to meet the goal.

51. Graph the equation. Does this equation represent a function? Explain.

52. If Latonya sells 100 magazine subscriptions and 200 newspaper subscriptions, will she meet her goal? Explain.

53. **Open Ended** Write an equation of a line with an \( x \)-intercept of 2.

54. **Reasoning** Explain why \( f(x) = \frac{x+2}{2} \) is a linear function.

**Challenge** For Exercises 55 and 56, use \( x + y = 0, x + y = 5, \) and \( x + y = -5. \)

55. Graph the equations. Then compare and contrast the graphs.

56. Write a linear equation whose graph is between the graphs of \( x + y = 0 \) and \( x + y = 5. \)

57. **Reasoning** Explain why the graph of \( x + 3y = 0 \) has only one intercept.

58. **Writing in Math** Use the information about study time on page 66 to explain how linear equations relate to time spent studying. Explain why only the part of the graph in the first quadrant is shown and an interpretation of the graph’s intercepts in terms of the situation.

**Standards Practice**

59. **ACT/SAT** Which function is linear?
   - A \( f(x) = x^2 \)
   - B \( g(x) = 2.7 \)
   - C \( f(x) = \sqrt{9-x^2} \)
   - D \( g(x) = \sqrt{x-1} \)

60. **Review** What is the complete solution to the equation?
   - \( |9-3x| = 18 \)
   - F \( x = -9; x = 3 \)
   - H \( x = -3; x = 9 \)
   - G \( x = -9; x = -3 \)
   - J \( x = 3; x = 9 \)

**Spiral Review**

State the domain and range of each relation. Then graph the relation and determine whether it is a function. (Lesson 2-1)

61. \{(-1, 5), (1, 3), (2, -4), (4, 3)\}

62. \{(0, 2), (1, 3), (2, -1), (1, 0)\}

Solve each inequality. (Lesson 1-6)

63. \(-2 < 3x + 1 < 7\)

64. \(|x + 4| > 2\)

65. **TAX** Including a 6% sales tax, a paperback book costs $8.43. What is the price before tax? (Lesson 1-3)

**Get Ready for the Next Lesson**

**PREREQUISITE SKILL** Find the reciprocal of each number.

66. \(-4\)

67. \(\frac{1}{2}\)

68. \(\frac{3}{4}\)

69. \(-1.25\)
The grade of a road is a percent that measures the steepness of the road. It is found by dividing the amount the road rises by the corresponding horizontal distance.

**Example**

Find Slope and Use Slope to Graph

Find the slope of the line that passes through \((-1, 4)\) and \((1, -2)\). Then graph the line.

\[
m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Slope formula}
\]

\[
m = \frac{-2 - 4}{1 - (-1)} = \frac{-6}{2} = -3
\]

The slope is \(-3\).
Graph the two ordered pairs and draw the line. Use the slope to check your graph by selecting any point on the line. Then go down 3 units and right 1 unit or go up 3 units and left 1 unit. This point should also be on the line.

**CHECK Your Progress**

1. Find the slope of the line that passes through \((1, -3)\) and \((3, 5)\). Then graph the line.

The slope of a line tells the direction in which it rises or falls.

**CONCEPT SUMMARY**

<table>
<thead>
<tr>
<th>Condition</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>If the line rises to the right, then the slope is positive.</td>
<td><img src="image1" alt="Graph" /></td>
</tr>
<tr>
<td>( m = \frac{y_2 - y_1}{x_2 - x_1} )</td>
<td>( y = 2x + 3 )</td>
</tr>
<tr>
<td>If the line is horizontal, then the slope is zero.</td>
<td><img src="image2" alt="Graph" /></td>
</tr>
<tr>
<td>( m = \frac{y_2 - y_1}{x_2 - x_1} )</td>
<td>( y = 2 )</td>
</tr>
<tr>
<td>If the line falls to the right, then the slope is negative.</td>
<td><img src="image3" alt="Graph" /></td>
</tr>
<tr>
<td>( m = \frac{y_2 - y_1}{x_2 - x_1} )</td>
<td>( y = -2x + 1 )</td>
</tr>
<tr>
<td>If the line is vertical, then the slope is undefined.</td>
<td><img src="image4" alt="Graph" /></td>
</tr>
<tr>
<td>( x = 2 )</td>
<td>( y = 3x + 1 )</td>
</tr>
</tbody>
</table>

**Real-World Example**

**Basketball** Refer to the graph at the right. Find the rate of change of the number of people attending Seattle Sonics home games from 1993 to 1996.

\[
\begin{align*}
  m &= \frac{y_2 - y_1}{x_2 - x_1} \\
  &= \frac{700 - 601}{1996 - 1993} \\
  &= \frac{99}{3} \\
  &\approx 33 \\
\end{align*}
\]

Between 1993 and 1996, the number of people attending Seattle Sonics home games increased at an average rate of about 33(1000) or 33,000 people per year.

**CHECK Your Progress**

2. In 1999, 45,616 students applied for admission to UCLA. In 2004, 56,878 students applied. Find the rate of change in the number of students applying for admission from 1999 to 2004.
Parallel and Perpendicular Lines  A family of graphs is a group of graphs that displays one or more similar characteristics. The parent graph is the simplest of the graphs in a family.

**GRAPHING CALCULATOR LAB**

**Lines with the Same Slope**

The calculator screen shows the graphs of $y = 3x$, $y = 3x + 2$, $y = 3x - 2$, and $y = 3x + 5$.

**THINK AND DISCUSS**

1. What is similar about the graphs? What is different about the graphs?

2. Write another function that has the same characteristics as these graphs. Check by graphing.

In the Lab, you saw that lines that have the same slope are parallel.

**Study Tip**

**Horizontal Lines**

All horizontal lines are parallel because they all have a slope of 0.

**KEY CONCEPT**

**Parallel Lines**

<table>
<thead>
<tr>
<th>Words</th>
<th>Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>In a plane, nonvertical lines with the same slope are parallel. All vertical lines are parallel.</td>
<td><img src="image" alt="Parallel Lines Diagram" /></td>
</tr>
</tbody>
</table>

**EXAMPLE**

Parallel Lines

Graph the line through $(-1, 3)$ that is parallel to the line with equation $x + 4y = -4$.

The $x$-intercept is $-4$, and the $y$-intercept is $-1$. Use the intercepts to graph $x + 4y = -4$.

The line falls 1 unit for every 4 units it moves to the right, so the slope is $-\frac{1}{4}$.

Now use the slope and the point at $(-1, 3)$ to graph the line parallel to the graph of $x + 4y = -4$.

3. Graph the line through $(-2, 4)$ that is parallel to the line with equation $x - 3y = 3$.

The graphs of $\overrightarrow{AB}$ and $\overrightarrow{CD}$ are perpendicular.

\[
\text{slope of line } AB \quad \text{slope of line } CD
\]

\[
\frac{-3 - 1}{-4 - 2} = \frac{-4}{-6} \quad \frac{-4 - 2}{1 - (-3)} = \frac{-6}{4} \quad \text{or} \quad \frac{-3}{2}
\]

The slopes are opposite reciprocals of each other. The product of the slopes of two perpendicular lines is always $-1$.

**Personal Tutor at ca.algebra2.com**

**Extra Examples at ca.algebra2.com**
**Oblique**

An oblique line is a line that is neither horizontal nor vertical.

---

**Perpendicular Lines**

Words: In a plane, two oblique lines are perpendicular if and only if the product of their slopes is $-1$.

Symbols: Suppose $m_1$ and $m_2$ are the slopes of two oblique lines. Then the lines are perpendicular if and only if $m_1m_2 = -1$, or $m_1 = -\frac{1}{m_2}$.

---

**EXAMPLE**

Perpendicular Lines

Graph the line through $(-3, 1)$ that is perpendicular to the line with equation $2x + 5y = 10$.

The $x$-intercept is 5, and the $y$-intercept is 2. Use the intercepts to graph $2x + 5y = 10$.

The line falls 2 units for every 5 units it moves to the right, so the slope is $-\frac{2}{5}$. The slope of the perpendicular line is the opposite reciprocal of $-\frac{2}{5}$, or $\frac{5}{2}$.

Start at $(-3, 1)$ and go up 5 units and right 2 units. Use this point and $(-3, 1)$ to graph the line.

4. Graph the line through $(-6, 2)$ that is perpendicular to the line with equation $3x - 2y = 6$.

---

**Check Your Progress**

**Example 1** (pp. 71–72)

Find the slope of the line that passes through each pair of points.

1. $(-2, -1), (2, -3)$  

2. $(2, 2), (4, 2)$  

3. $(4, 5), (-1, 0)$

Graph the line passing through the given point with the given slope.

4. $(2, -1), -3$  

5. $(-3, -4), \frac{3}{2}$

**Example 2** (p. 72)

**WEATHER** For Exercises 6–8, use the table that shows the temperatures at different times on the same day.

<table>
<thead>
<tr>
<th>Time</th>
<th>8:00 A.M.</th>
<th>10:00 A.M.</th>
<th>12:00 P.M.</th>
<th>2:00 P.M.</th>
<th>4:00 P.M.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temp (°F)</td>
<td>36</td>
<td>47</td>
<td>55</td>
<td>58</td>
<td>60</td>
</tr>
</tbody>
</table>

6. What was the average rate of change of the temperature from 8:00 A.M. to 10:00 A.M.?

7. What was the average rate of change of the temperature from 12:00 P.M. to 4:00 P.M.?

8. During what 2-hour period was the average rate of change of the temperature the least?
Find the slope of the line that passes through each pair of points.

13. \((4, -1), (6, -6)\)
14. \((-8, -3), (2, 3)\)
15. \((8, 7), (7, -6)\)
16. \((-2, -3), (0, -5)\)
17. \((4, 9), (11, 9)\)
18. \((4, -1.5), (4, 4.5)\)

Graph the line passing through the given point with the given slope.

19. \((-1, 4), m = \frac{2}{3}\)
20. \((-3, -1), m = -\frac{1}{5}\)
21. \((3, -4), m = 2\)
22. \((1, 2), m = -3\)
23. \((6, 2), m = 0\)
24. \((-2, -3), \text{undefined}\)

**CAMERAS** For Exercises 25 and 26, refer to the graph that shows the number of digital still cameras and film cameras sold in recent years.

25. Find the average rate of change of the number of digital cameras sold from 1999 to 2003.
26. Find the average rate of change of the number of film cameras sold from 1999 to 2003. What does the sign of the rate mean?

**TRAVEL** For Exercises 27–29, use the following information. Mr. and Mrs. Wellman are taking their daughter to college. The table shows their distance from home after various amounts of time.

27. Find the average rate of change of their distance from home between 1 and 3 hours after leaving home.
28. Find the average rate of change of their distance from home between 0 and 5 hours after leaving home.
29. What is another word for rate of change in this situation?

Graph the line that satisfies each set of conditions.

30. passes through \((-2, 2)\), parallel to a line whose slope is \(-1\)
31. passes through \((2, -5)\), parallel to graph of \(x = 4\)
32. passes through \((2, -1)\), parallel to graph of \(x + y = 10\)
33. passes through \((2, -1)\), parallel to graph of \(2x + 3y = 6\)
34. passes through \((2, -1)\), perpendicular to graph of \(2x + 3y = 6\)
35. passes through \((-4, 1)\), perpendicular to a line whose slope is \(-\frac{3}{2}\)
36. passes through \((3, 3)\), perpendicular to graph of \(y = 3\)
37. passes through \((0, 0)\), perpendicular to graph of \(y = -x\)
Find the slope of the line that passes through each pair of points.

38. \( \left( \frac{1}{2} , -\frac{1}{3} \right) , \left( \frac{1}{4} , \frac{2}{3} \right) \)  
39. \( \left( \frac{1}{2} , \frac{2}{3} \right) , \left( \frac{5}{6} , \frac{1}{4} \right) \)
40. \((c, 5), (c, -2)\)  
41. \((3, d), (-5, d)\)

42. **WASHINGTON MONUMENT**  The Washington Monument, in Washington, D.C., is 555 feet \(\frac{5}{8}\) inches tall and weighs 90,854 tons. The monument is topped by a square aluminum pyramid. The sides of the pyramid’s base measure 5.6 inches, and the pyramid is 8.9 inches tall. Estimate the slope that a face of the pyramid makes with its base.

43. Determine the value of \(r\) so that the line through \((5, r)\) and \((2, 3)\) has slope 2.
44. Determine the value of \(r\) so that the line through \((6, r)\) and \((9, 2)\) has slope \(\frac{1}{3}\).

Graph the line that satisfies each set of conditions.

45. perpendicular to graph of \(3x - 2y = 24\), intersects that graph at its \(x\)-intercept
46. perpendicular to graph of \(2x + 5y = 10\), intersects that graph at its \(y\)-intercept

47. **GEOMETRY** Determine whether quadrilateral \(ABCD\) with vertices \(A(-2, -1)\), \(B(1, 1)\), \(C(3, -2)\), and \(D(0, -4)\) is a rectangle. Explain.

For Exercises 48 and 49, use a graphing calculator to investigate the graphs of each set of equations. Explain how changing the slope affects the graph of the line.

48. \(y = 2x + 3, y = 4x + 3, y = 8x + 3, y = x + 3\)
49. \(y = -3x + 1, y = -x + 1, y = -5x + 1, y = -7x + 1\)

50. **OPEN ENDED** Write an equation of a line with slope 0. Describe the graph of the equation.

51. **CHALLENGE** If the graph of the equation \(ax + 3y = 9\) is perpendicular to the graph of the equation \(3x + y = -4\), find the value of \(a\).

52. **FIND THE ERROR** Gabriel and Luisa are finding the slope of the line through \((2, 4)\) and \((-1, 5)\). Who is correct? Explain your reasoning.

\[
\begin{align*}
\text{Gabriel} &: m = \frac{5-4}{2-(-1)} = \frac{1}{3} \\
\text{Luisa} &: m = \frac{4-5}{2-(-1)} = \frac{-1}{3}
\end{align*}
\]

53. **REASONING** Determine whether the statement *A line has a slope that is a real number is sometimes, always, or never true.* Explain your reasoning.

54. **Writing in Math** Use the information about the grade of a road on page 71 to explain how slope applies to the steepness of roads. Include a graph of \(y = 0.08x\), which corresponds to a grade of 8%.
Find the x-intercept and the y-intercept of the graph of each equation. Then graph the equation. (Lesson 2-2)

57. 
\[ -2x + 5y = 20 \]

58. 
\[ 4x - 3y + 8 = 0 \]

59. 
\[ y = 7x \]

Find each value if \( f(x) = 3x - 4 \). (Lesson 2-1)

60. 
\[ f(-1) \]

61. 
\[ f(3) \]

62. 
\[ f\left(\frac{1}{2}\right) \]

63. 
\[ f(a) \]

Solve each inequality. (Lessons 1-5 and 1-6)

64. 
\[ 5 < 2x + 7 < 13 \]

65. 
\[ 2z + 5 \geq 1475 \]

66. SCHOOL A test has multiple-choice questions worth 4 points each and true-false questions worth 3 points each. Marco answers 14 multiple-choice questions correctly. How many true-false questions must he answer correctly to get at least 80 points total? (Lesson 1-5)

Simplify. (Lessons 1-1 and 1-2)

67. 
\[ \frac{1}{3}(15a + 9b) - \frac{1}{7}(28b - 84a) \]

68. 
\[ 3 + (21 \div 7) \times 8 \div 4 \]

PREREQUISITE SKILL Solve each equation for \( y \). (Lesson 1-3)

69. 
\[ x + y = 9 \]

70. 
\[ 4x + y = 2 \]

71. 
\[ -3x - y + 7 = 0 \]

72. 
\[ 5x - 2y - 1 = 0 \]

73. 
\[ 3x - 5y + 4 = 0 \]

74. 
\[ 2x + 3y - 11 = 0 \]
Graphing Calculator Lab
The Family of Linear Functions

The parent function of the family of linear functions is \( f(x) = x \). You can use a graphing calculator to investigate how changing the parameters \( m \) and \( b \) in \( f(x) = mx + b \) affects the graphs as compared to the parent function.

### Activity 1: \( b \) in \( f(x) = mx + b \)

Graph \( f(x) = x \), \( f(x) = x + 3 \), and \( f(x) = x - 5 \) in the standard viewing window.

Enter the equations in the \( Y= \) list as \( Y_1 \), \( Y_2 \), and \( Y_3 \). Then graph the equations.

**Keystrokes:**

\[
y= x,\ T,\ 0,\ n\ \ \text{ENTER} \ \ x,\ T,\ 0,\ n\ \ +\ 3\ \ \text{ENTER} \ \ x,\ T,\ 0,\ n\ \ -\ 5\ \ \text{ENTER}
\]

1A. Compare and contrast the graphs.
1B. How would you obtain the graphs of \( f(x) = x + 3 \) and \( f(x) = x - 5 \) from the graph of \( f(x) = x \)?

The parameter \( m \) in \( f(x) = mx + b \) affects the graphs in a different way than \( b \).

### Activity 2: \( m \) in \( f(x) = mx + b \)

Graph \( f(x) = x \), \( f(x) = 3x \), and \( f(x) = \frac{1}{2}x \) in the standard viewing window.

Enter the equations in the \( Y= \) list and graph.

2A. How do the graphs compare?
2B. Which graph is steepest? Which graph is the least steep?
2C. Graph \( f(x) = -x \), \( f(x) = -3x \), and \( f(x) = -\frac{1}{2}x \) in the standard viewing window. How do these graphs compare?

### Analyze the Results

Graph each set of equations on the same screen. Describe the similarities or differences among the graphs.

1. \( f(x) = 3x \)
   - \( f(x) = 3x + 1 \)
   - \( f(x) = 3x - 2 \)
2. \( f(x) = x + 2 \)
   - \( f(x) = 5x + 2 \)
   - \( f(x) = \frac{1}{2}x + 2 \)
3. \( f(x) = x - 3 \)
   - \( f(x) = 2x - 3 \)
   - \( f(x) = 0.75x - 3 \)
4. What do the graphs of equations of the form \( f(x) = mx + b \) have in common?
5. How do the values of \( b \) and \( m \) affect the graph of \( f(x) = mx + b \) as compared to the parent function \( f(x) = x \)?
6. Summarize your results. How can knowing about the effects of \( m \) and \( b \) help you sketch the graph of a function?
Lesson 2-4

Writing Linear Equations

Main Ideas

• Write an equation of a line given the slope and a point on the line.
• Write an equation of a line parallel or perpendicular to a given line.

Reinforcement of Algebra I Standard 7.0 Students verify that a point lies on a line, given an equation of the line. Students are able to derive linear equations by using the point-slope formula. (Key, CAHSEE)

New Vocabulary

slope-intercept form
point-slope form

GET READY for the Lesson

When a company manufactures a product, they must consider two types of cost. There is the fixed cost, which they must pay no matter how many of the product they produce, and there is variable cost, which depends on how many of the product they produce. In some cases, the total cost can be found using a linear equation such as

\[ y = 5400 + 1.37x. \]

Forms of Equations

Consider the graph at the right. The line passes through \( A(0, b) \) and \( C(x, y) \). Notice that \( b \) is the \( y \)-intercept of \( AC \). You can use these two points to find the slope of \( AC \).

Substitute the coordinates of points \( A \) and \( C \) into the slope formula.

\[
m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Slope formula}
\]

\[
m = \frac{y - b}{x - 0} \quad (x_1, y_1) = (0, b), \ (x_2, y_2) = (x, y)
\]

\[
m = \frac{y - b}{x} \quad \text{Simplify.}
\]

Now solve the equation for \( y \).

\[
mx = y - b \quad \text{Multiply each side by} \ x.
\]

\[
mx + b = y \quad \text{Add} \ b \ \text{to each side.}
\]

\[
y = mx + b \quad \text{Symmetric Property of Equality}
\]

When an equation is written in this form, it is in slope-intercept form.

Key Concept

Slope-Intercept Form of a Linear Equation

Words

The slope-intercept form of the equation of a line is \( y = mx + b \), where \( m \) is the slope and \( b \) is the \( y \)-intercept.

Symbols

\[ y = mx + b \]

Model

If you are given the slope and \( y \)-intercept of a line, you can find an equation of the line by substituting the values of \( m \) and \( b \) into the slope-intercept form. You can also use the slope-intercept form to find an equation of a line if you know the slope and the coordinates of any point on the line.
EXAMPLE 1 Write an Equation Given Slope and a Point

Write an equation in slope-intercept form for the line that has a slope of \(- \frac{3}{2}\) and passes through \((-4, 1)\).

\[
y = mx + b \quad \text{Slope-intercept form}
\]

\[
1 = \frac{3}{2}(-4) + b \quad (x, y) = (-4, 1), \; m = \frac{3}{2}
\]

\[
1 = 6 + b \quad \text{Simplify.}
\]

\[
-5 = b \quad \text{Subtract 6 from each side.}
\]

The equation in slope-intercept form is \(y = -\frac{3}{2}x - 5\).

Write an equation in slope-intercept form for the line that satisfies each set of conditions.

1A. slope \(\frac{4}{3}\), passes through \((3, 2)\)  
1B. slope \(-4\), passes through \((-2, -2)\)

If you are given the coordinates of two points on a line, you can use the point-slope form to find an equation of the line that passes through them.

KEY CONCEPT Point-Slope Form of a Linear Equation

<table>
<thead>
<tr>
<th>Words</th>
<th>Symbols</th>
</tr>
</thead>
<tbody>
<tr>
<td>The point-slope form of the equation of a line is (y - y_1 = m(x - x_1)), where ((x_1, y_1)) are the coordinates of a point on the line and (m) is the slope of the line.</td>
<td>(y - y_1 = m(x - x_1))</td>
</tr>
</tbody>
</table>

STANDARDS PRACTICE Write an Equation Given Two Points

What is an equation of the line through \((-1, 4)\) and \((-4, 5)\)?

A. \(y = \frac{1}{3}x + \frac{11}{3}\)  
B. \(y = \frac{1}{3}x + \frac{13}{3}\)  
C. \(y = -\frac{1}{3}x + \frac{13}{3}\)  
D. \(y = -3x + 1\)

Read the Item

You are given the coordinates of two points on the line.

Solve the Item

First, find the slope of the line.

\[
m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Slope formula}
\]

\[
= \frac{5 - 4}{-4 - (-1)} \quad (x_1, y_1) = (-1, 4), \quad (x_2, y_2) = (-4, 5)
\]

\[
= \frac{1}{3} \quad \text{or} \quad -\frac{1}{3} \quad \text{Simplify.}
\]

Then write an equation.

\[
y - y_1 = m(x - x_1) \quad \text{Point-slope form}
\]

\[
y - 4 = -\frac{1}{3}[x - (-1)] \quad m = -\frac{1}{3}; \text{use either point for } (x, y).
\]

\[
y = -\frac{1}{3}x + \frac{11}{3} \quad \text{The answer is A.}
\]

2. What is an equation of the line through \((2, 3)\) and \((-4, -5)\)?

F. \(y = \frac{4}{3}x + \frac{1}{3}\)  
G. \(y = \frac{4}{3}x + 8\)  
H. \(y = \frac{1}{3}x + \frac{17}{3}\)  
J. \(y = \frac{1}{3}x - 8\)
When changes in real-world situations occur at a linear rate, a linear equation can be used as a model for describing the situation.

**SALES**  As a salesperson, Eric Fu is paid a daily salary plus commission. When his sales are $1000, he makes $100. When his sales are $1400, he makes $120.

**a.** Write a linear equation to model this situation.

Let $x$ be his sales and let $y$ be the amount of money he makes. Use the points $(1000, 100)$ and $(1400, 120)$ to make a graph to represent the situation.

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Slope formula}$$

$$= \frac{120 - 100}{1400 - 1000} \quad (x_1, y_1) = (1000, 100), \quad (x_2, y_2) = (1400, 120)$$

$$= 0.05 \quad \text{Simplify.}$$

Now use the slope and either of the given points with the point-slope form to write the equation.

$$y - y_1 = m(x - x_1) \quad \text{Point-slope form}$$

$$(y - 100) = 0.05(x - 1000) \quad m = 0.05, \quad (x_1, y_1) = (1000, 100)$$

$$y - 100 = 0.05x - 50 \quad \text{Distributive Property}$$

$$y = 0.05x + 50 \quad \text{Add 100 to each side.}$$

The slope-intercept form of the equation is $y = 0.05x + 50$.

**b.** What are Mr. Fu’s daily salary and commission rate?

The $y$-intercept of the line is 50. The $y$-intercept represents the money Eric would make if he had no sales. In other words, $50 is his daily salary. The slope of the line is 0.05. Since the slope is the coefficient of $x$, which is his sales, he makes 5% commission.

**c.** How much would Mr. Fu make in a day if his sales were $2000?

Find the value of $y$ when $x = 2000$.

$$y = 0.05x + 50 \quad \text{Use the equation you found in part a.}$$

$$= 0.05(2000) + 50 \quad \text{Replace } x \text{ with 2000.}$$

$$= 100 + 50 \text{ or 150} \quad \text{Simplify.}$$

Mr. Fu would make $150 if his sales were $2000.

**SCHOOL CLUBS**  For each meeting of the Putnam High School book club, $25 is taken from the activities account to buy snacks and materials. After their sixth meeting, there will be $350 left in the activities account.

**3A.** If no money is put back into the account, what equation can be used to show how much money is left in the activities account after having $x$ number of meetings?

**3B.** How much money was originally in the account?

**3C.** After how many meetings will there be no money left in the activities account?
Parallel and Perpendicular Lines  The slope-intercept and point-slope forms can be used to find equations of lines that are parallel or perpendicular to given lines.

**EXAMPLE Write an Equation of a Perpendicular Line**

4 Write an equation for the line that passes through \((-4, 3)\) and is perpendicular to the line whose equation is \(y = -4x - 1\).

The slope of the given line is \(-4\). Since the slopes of perpendicular lines are opposite reciprocals, the slope of the perpendicular line is \(\frac{1}{4}\).

Use the point-slope form and the ordered pair \((-4, 3)\).

\[
y - y_1 = m(x - x_1) \quad \text{Point-slope form}
\]

\[
y - 3 = \frac{1}{4}[x - (-4)] \quad (x_1, y_1) = (-4, 3), m = \frac{1}{4}
\]

\[
y - 3 = \frac{1}{4}x + 1 \quad \text{Distributive Property}
\]

\[
y = \frac{1}{4}x + 4 \quad \text{Add 3 to each side.}
\]

4. Write an equation for the line that passes through \((3, 7)\) and is perpendicular to the line whose equation is \(y = \frac{3}{4}x - 5\).

**Check Your Understanding**

Write an equation in slope-intercept form for the line that satisfies each set of conditions.

**Example 1** (p. 80)

1. slope 0.5, passes through \((6, 4)\)  
2. slope \(-\frac{3}{4}\), passes through \((2, \frac{1}{2})\)  
3. slope 3, passes through \((0, -6)\)  
4. slope 0.25, passes through \((0, 4)\)  
5. passes through \((6, 1)\) and \((8, -4)\)  
6. passes through \((-3, 5)\) and \((2, 2)\)

Write an equation in slope-intercept form for each graph.

7.  
8.  

9. **STANDARDS PRACTICE** What is an equation of the line through \((2, -4)\) and \((-3, -1)\)?

   A. \(y = -\frac{3}{5}x + \frac{26}{5}\)  
   B. \(y = -\frac{3}{5}x - \frac{14}{5}\)

   C. \(y = \frac{3}{5}x - \frac{26}{5}\)  
   D. \(y = \frac{3}{5}x + \frac{14}{5}\)

**Example 3** (p. 81)

10. **PART-TIME JOB** Each week Carmen earns $15 plus $0.17 for every pamphlet that she delivers. Write an equation that can be used to find how much Carmen earns each week. How much will she earn the week she delivers 300 pamphlets?
Write an equation in slope-intercept form for the line that satisfies each set of conditions.

11. perpendicular to \( y = \frac{3}{4}x - 2 \), passes through \( (2, 0) \)
12. perpendicular to \( y = \frac{1}{2}x + 6 \), passes through \( (-5, 7) \)

Write an equation in slope-intercept form for the line that satisfies each set of conditions.

13. slope 3, passes through \( (0, -6) \)
14. slope 0.25, passes through \( (0, 4) \)
15. slope \(-\frac{1}{2}\), passes through \( (1, 3) \)
16. slope \( \frac{3}{2} \) passes through \( (-5, 1) \)
17. passes through \( (-2, 5) \) and \( (3, 1) \)
18. passes through \( (7, 1) \) and \( (7, 8) \)
19. passes through \( (4, 6) \), parallel to the graph of \( y = \frac{2}{3}x + 5 \)
20. passes through \( (2, -5) \), perpendicular to the graph of \( y = \frac{1}{4}x + 7 \)

Write an equation in slope-intercept form for each graph.

21.

\[ \begin{array}{c|c}
\text{x} & \text{y} \\
\hline
0 & 0 \\
-2 & -4 \\
\end{array} \]

22.

\[ \begin{array}{c|c}
\text{x} & \text{y} \\
\hline
0 & 2 \\
2 & 4 \\
\end{array} \]

23. **ECOLOGY** A park ranger at Creekside Woods estimates there are 6000 deer in the park. She also estimates that the population will increase by 75 deer each year to come. Write an equation that represents how many deer will be in the park in \( x \) years.

24. **BUSINESS** For what distance do the two stores charge the same amount for a balloon arrangement?

**REAL-WORLD LINK**

The number of whitetail deer in the United States increased from about half a million in the early 1900s to 25 to 30 million in 2005.

**Source:** espn.com

**GEOMETRY** For Exercises 25–27, use the equation \( d = 180(c - 2) \) that gives the total number of degrees \( d \) in any convex polygon with \( c \) sides.

25. Write this equation in slope-intercept form.
26. Identify the slope and \( d \)-intercept.
27. Find the number of degrees in a pentagon.

**SCIENCE** For Exercises 28–30, use the following information.

Ice forms at a temperature of 0°C, which corresponds to a temperature of 32°F.

A temperature of 100°C corresponds to a temperature of 212°F.

28. Write and graph the linear equation that gives the number \( y \) of degrees Fahrenheit in terms of the number \( x \) of degrees Celsius.
29. What temperature corresponds to 20°C?
30. What temperature is the same on both scales?
Write an equation in slope-intercept form for the line that satisfies each set of conditions.

31. slope \(-0.5\), passes through \((2, -3)\)  
32. slope \(4\), passes through the origin  
33. \(x\)-intercept \(-4\), \(y\)-intercept \(4\)  
34. \(x\)-intercept \(\frac{1}{3}\), \(y\)-intercept \(-\frac{1}{4}\)  
35. passes through \((6, -5)\), perpendicular to the line whose equation is \(3x - \frac{1}{5}y = 3\)  
36. passes through \((-3, -1)\), parallel to the line that passes through \((3, 3)\) and \((0, 6)\)

37. OPEN ENDED Write an equation of a line in slope-intercept form.

38. REASONING What are the slope and \(y\)-intercept of the equation \(cx + y = d\)?

39. CHALLENGE Given \(\triangle ABC\) with vertices \(A(-6, -8)\), \(B(6, 4)\), and \(C(-6, 10)\), write an equation of the line containing the altitude from \(A\). (Hint: The altitude from \(A\) is a segment that is perpendicular to \(\overline{BC}\).)

40. Writing in Math Use the information on page 79 to explain how linear equations apply to business. Relate the terms fixed cost and variable cost to the equation \(y = 5400 + 1.37x\), where \(y\) is the cost to produce \(x\) units of a product. Give the cost to produce 1000 units of the product.

### ACT/SAT

41. What is an equation of the line through \(\left(\frac{1}{2}, -\frac{3}{2}\right)\) and \(\left(-\frac{1}{2}, \frac{1}{2}\right)\)?

A. \(y = -2x - \frac{1}{2}\)  
B. \(y = -3x\)  
C. \(y = 2x - \frac{5}{2}\)  
D. \(y = \frac{1}{2}x + 1\)

### REVIEW

42. The total cost \(c\) in dollars to go to a fair and ride \(n\) roller coasters is given by the equation \(c = 15 + 3n\). If the total cost was $33, how many roller coasters were ridden?

F. 6  
G. 7  
H. 8  
J. 9

### Spiral Review

Find the slope of the line that passes through each pair of points. (Lesson 2-3)

43. \((7, 2), (5, 6)\)  
44. \((1, -3), (3, 3)\)  
45. \((-5, 0)\), \((4, 0)\)

46. INTERNET A Webmaster estimates that the time (seconds) to connect to the server when \(n\) people are connecting is given by \(t(n) = 0.005n + 0.3\). Estimate the time to connect when 50 people are connecting. (Lesson 2-2)

Solve each inequality. (Lessons 1-5 and 1-6)

47. \(|x - 2| \leq -99\)  
48. \(-4x + 7 \leq 31\)  
49. \(2(r - 4) + 5 \geq 9\)

### PREREQUISITE SKILL

Find the median of each set of numbers. (Page 760)

50. \{3, 2, 1, 3, 4, 8, 4\}  
51. \{9, 3, 7, 5, 6, 3, 7, 9\}  
52. \{138, 235, 976, 230, 412, 466\}  
53. \{2.5, 7.8, 5.5, 2.3, 6.2, 7.8\}
1. State the domain and range of the relation \{(2, 5), (−3, 2), (2, 1), (−7, 4), (0, −2)\}. Is the relation a function? Write yes or no. (Lesson 2-1)

2. Find \(f(15)\) if \(f(x) = 100x − 5x^2\). (Lesson 2-1)

For Exercises 3–5, use the table that shows a teacher’s class size in recent years. (Lesson 2-1)

<table>
<thead>
<tr>
<th>Year</th>
<th>Class Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>2002</td>
<td>27</td>
</tr>
<tr>
<td>2003</td>
<td>30</td>
</tr>
<tr>
<td>2004</td>
<td>29</td>
</tr>
<tr>
<td>2005</td>
<td>33</td>
</tr>
</tbody>
</table>

3. Graph the relation.

4. Identify the domain and range.

5. Is the relation a function? Explain your reasoning.

6. Write \(y = −6x + 4\) in standard form. Identify \(A, B,\) and \(C\). (Lesson 2-2)

7. Find the \(x\)-intercept and the \(y\)-intercept of the graph of \(3x + 5y = 30\). Then graph the equation. (Lesson 2-2)

8. **MULTIPLE CHOICE** What is the \(y\)-intercept of the graph of \(10 − x = 2y\)? (Lesson 2-2)
   - A 2
   - B 5
   - C 6
   - D 10

9. What is the slope of the line containing the points shown in the table? (Lesson 2-3)

<table>
<thead>
<tr>
<th>(x)</th>
<th>(y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>−1</td>
</tr>
<tr>
<td>8</td>
<td>7</td>
</tr>
<tr>
<td>15</td>
<td>15</td>
</tr>
</tbody>
</table>

10. Graph the line that passes through \((4, −3)\) and is parallel to the line with equation \(2x + 5y = 10\). (Lesson 2-3)

**SCHOOL** For Exercises 15 and 16, use the following information.
The graph shows the effect that education levels have on income. (Lesson 2-3)

15. Find the average rate of change of income for females that have 12 years of education to females that have 16+ years of education.

16. Find the average rate of change of income for males that have 12 years of education to males that have 16+ years of education.

17. Write an equation in slope-intercept form of the line with slope \(−\frac{2}{3}\) that passes through the point \((-3, 5)\). (Lesson 2-4)

18. **MULTIPLE CHOICE** Find the equation of the line that passes through \((0, −3)\) and \((4, 1)\). (Lesson 2-4)
   - F \(y = −x + 3\)
   - G \(y = −x − 3\)
   - H \(y = x − 3\)
   - J \(y = x + 3\)

**PART-TIME JOB** Jesse is a pizza delivery driver. Each day his employer gives him \$20 plus \$0.50 for every pizza that he delivers. (Lesson 2-4)

19. Write an equation that can be used to determine how much Jesse earns each day if he delivers \(x\) pizzas.

20. How much will he earn the day he delivers 20 pizzas?
The table shows the number of Calories burned per hour by a 140-pound person running at various speeds. A linear function can be used to model these data.

<table>
<thead>
<tr>
<th>Speed (mph)</th>
<th>Calories</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>508</td>
</tr>
<tr>
<td>6</td>
<td>636</td>
</tr>
<tr>
<td>7</td>
<td>731</td>
</tr>
<tr>
<td>8</td>
<td>858</td>
</tr>
</tbody>
</table>

**Scatter Plots** Data with two variables, such as speed and Calories, is called bivariate data. A set of bivariate data graphed as ordered pairs in a coordinate plane is called a scatter plot. A scatter plot can show whether there is a positive, negative, or no correlation between the data.

The more closely data can be approximated by a line, the stronger the correlation. Correlations are usually described as strong or weak.

**Prediction Equations** When you find a line that closely approximates a set of data, you are finding a line of fit for the data. An equation of such a line is often called a prediction equation because it can be used to predict one of the variables given the other variable.

To find a line of fit and a prediction equation for a set of data, select two points that appear to represent the data well. This is a matter of personal judgment, so your line and prediction equation may be different from someone else’s.
Lesson 2-5
Statistics: Using Scatter Plots

Choosing the Independent Variable

Letting \( x \) be the number of years since the first year in the data set sometimes simplifies the calculations involved in finding a function to model the data.

Find and Use a Prediction Equation

HOUSING The table below shows the median selling price of new, privately-owned, one-family houses for some recent years.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Price ($1000)</td>
<td>130.0</td>
<td>140.0</td>
<td>152.5</td>
<td>169.0</td>
<td>187.6</td>
<td>219.6</td>
</tr>
</tbody>
</table>

Source: U.S. Census Bureau and U.S. Department of Housing and Urban Development

a. Draw a scatter plot and a line of fit for the data. How well does the line fit the data?

Graph the data as ordered pairs, with the number of years since 1994 on the horizontal axis and the price on the vertical axis. The points (2, 140.0) and (8, 187.6) appear to represent the data well. Draw a line through these two points. Except for (10, 219.6), this line fits the data very well.

b. Find a prediction equation. What do the slope and \( y \)-intercept indicate?

Find an equation of the line through (2, 140.0) and (8, 187.6).

\[
\begin{align*}
m &= \frac{y_2 - y_1}{x_2 - x_1} \\
&= \frac{187.6 - 140.0}{8 - 2} \\
&\approx 7.93
\end{align*}
\]

Point-slope form

\[
\begin{align*}
y - y_1 &= m(x - x_1) \\
y - 140.0 &= 7.93(x - 2) \\
y &= 7.93x - 15.86 \\
y &= 7.93x + 124.14
\end{align*}
\]

One prediction equation is \( y = 7.93x + 124.14 \). The slope indicates that the median price is increasing at a rate of about $7930 per year. The \( y \)-intercept indicates that, according to the trend of the rest of the data, the median price in 1994 should have been about $124,140.

c. Predict the median price in 2014.

The year 2014 is 20 years after 1994, so use the prediction equation to find the value of \( y \) when \( x = 20 \).

\[
\begin{align*}
y &= 7.93x + 124.14 \\
y &= 7.93(20) + 124.14 \\
y &= 282.74
\end{align*}
\]

The model predicts that the median price in 2014 will be about $282,740.

(continued on the next page)
d. How accurate does the prediction appear to be?

Except for the outlier, the line fits the data very well, so the predicted value should be fairly accurate.

1. The table shows the mean selling price of new, privately owned one-family homes for some recent years. Draw a scatter plot and a line of fit for the data. Then find a prediction equation and predict the mean price in 2014.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Price ($1000)</td>
<td>154.5</td>
<td>166.4</td>
<td>181.9</td>
<td>207.0</td>
<td>228.7</td>
<td>273.5</td>
</tr>
</tbody>
</table>

Source: U.S. Census Bureau and U.S. Department of Housing and Urban Development

Personal Tutor at ca.algebra2.com

ALGEBRA LAB

Head versus Height

COLLECT AND ORGANIZE THE DATA

Collect data from several of your classmates. Measure the circumference of each person’s head and his or her height. Record the data as ordered pairs of the form (height, circumference).

ANALYZE THE DATA

1. Graph the data in a scatter plot and write a prediction equation.
2. Explain the meaning of the slope in the prediction equation.
3. Predict the head circumference of a person who is 66 inches tall.
4. Predict the height of an individual whose head circumference is 18 inches.

Example

(p. 87)

Complete parts a–c for each set of data in Exercises 1 and 2.

a. Draw a scatter plot and a line of fit, and describe the correlation.

b. Use two ordered pairs to write a prediction equation.

c. Use your prediction equation to predict the missing value.

1. SCIENCE The table shows the temperature in the atmosphere at various altitudes.

<table>
<thead>
<tr>
<th>Altitude (ft)</th>
<th>0</th>
<th>1000</th>
<th>2000</th>
<th>3000</th>
<th>4000</th>
<th>5000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temp (°C)</td>
<td>15.0</td>
<td>13.0</td>
<td>11.0</td>
<td>9.1</td>
<td>7.1</td>
<td>?</td>
</tr>
</tbody>
</table>

Source: NASA

2. TELEVISION The table shows the percentage of U.S. households with televisions that also had cable service in some recent years.

<table>
<thead>
<tr>
<th>Year</th>
<th>1995</th>
<th>1997</th>
<th>1999</th>
<th>2001</th>
<th>2003</th>
<th>2015</th>
</tr>
</thead>
<tbody>
<tr>
<td>Percent</td>
<td>65.7</td>
<td>67.3</td>
<td>68.0</td>
<td>69.2</td>
<td>68.0</td>
<td>?</td>
</tr>
</tbody>
</table>

Source: Nielsen Media Research
Complete parts a–c for each set of data in Exercises 3–6.

a. Draw a scatter plot and a line of fit, and describe the correlation.
b. Use two ordered pairs to write a prediction equation.
c. Use your prediction equation to predict the missing value.

3. SAFETY All states and the District of Columbia have enacted laws setting 21 as the minimum drinking age. The table shows the estimated cumulative number of lives these laws have saved by reducing traffic fatalities.

<table>
<thead>
<tr>
<th>Year</th>
<th>1999</th>
<th>2000</th>
<th>2001</th>
<th>2002</th>
<th>2003</th>
<th>2015</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lives (1000s)</td>
<td>19.1</td>
<td>20.0</td>
<td>21.0</td>
<td>21.9</td>
<td>22.8</td>
<td>?</td>
</tr>
</tbody>
</table>

Source: National Highway Traffic Safety Administration

4. HOCKEY The table shows the number of goals and assists for some of the members of the Detroit Red Wings in a recent NHL season.

<table>
<thead>
<tr>
<th>Goals</th>
<th>30</th>
<th>25</th>
<th>18</th>
<th>14</th>
<th>15</th>
<th>14</th>
<th>10</th>
<th>6</th>
<th>4</th>
<th>30</th>
<th>?</th>
</tr>
</thead>
<tbody>
<tr>
<td>Assists</td>
<td>49</td>
<td>43</td>
<td>33</td>
<td>32</td>
<td>28</td>
<td>29</td>
<td>12</td>
<td>9</td>
<td>15</td>
<td>38</td>
<td>20</td>
</tr>
</tbody>
</table>

Source: www.detroitredwings.com

5. HEALTH The table shows the number of gallons of bottled water consumed per person in some recent years.

<table>
<thead>
<tr>
<th>Year</th>
<th>1998</th>
<th>1999</th>
<th>2000</th>
<th>2001</th>
<th>2002</th>
<th>2003</th>
<th>2015</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gallons</td>
<td>15.0</td>
<td>16.4</td>
<td>17.4</td>
<td>18.8</td>
<td>20.7</td>
<td>22.0</td>
<td>?</td>
</tr>
</tbody>
</table>

Source: U.S. Department of Agriculture

6. THEATER The table shows the total revenue of all Broadway plays for recent seasons.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Revenue ($ millions)</td>
<td>603</td>
<td>666</td>
<td>643</td>
<td>721</td>
<td>771</td>
<td>?</td>
</tr>
</tbody>
</table>

Source: The League of American Theatres and Producers, Inc.

MEDICINE For Exercises 7–9, use the graph that shows how much Americans spent on health care in some recent years and a prediction for how much they will spend in 2014.

7. Write a prediction equation from the data for 1999 to 2003.
8. Use your equation to predict the amount for 2014.
9. Compare your prediction to the one given in the graph.

Source: cms.hhs.gov
**FINANCE** For Exercises 10 and 11, use the following information. Della has $1000 that she wants to invest in the stock market. She is considering buying stock in either Company 1 or Company 2. The values of the stocks at the end of each of the last 4 months are shown in the tables below.

10. Based only on these data, which stock should Della buy? Explain.

11. Do you think investment decisions should be based on this type of reasoning? If not, what other factors should be considered?

<table>
<thead>
<tr>
<th>Company 1</th>
<th>Share Price ($)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aug.</td>
<td>25.13</td>
</tr>
<tr>
<td>Sept.</td>
<td>22.94</td>
</tr>
<tr>
<td>Oct.</td>
<td>24.19</td>
</tr>
<tr>
<td>Nov.</td>
<td>22.56</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Company 2</th>
<th>Share Price ($)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aug.</td>
<td>31.25</td>
</tr>
<tr>
<td>Sept.</td>
<td>32.38</td>
</tr>
<tr>
<td>Oct.</td>
<td>32.06</td>
</tr>
<tr>
<td>Nov.</td>
<td>32.44</td>
</tr>
</tbody>
</table>

**PLANETS** For Exercises 12–15, use the table below that shows the average distance from the Sun and average temperature for eight of the planets.

<table>
<thead>
<tr>
<th>Planet</th>
<th>Average Distance from the Sun (million miles)</th>
<th>Average Temperature (°F)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mercury</td>
<td>36</td>
<td>333</td>
</tr>
<tr>
<td>Venus</td>
<td>67.2</td>
<td>867</td>
</tr>
<tr>
<td>Earth</td>
<td>93</td>
<td>59</td>
</tr>
<tr>
<td>Mars</td>
<td>141.6</td>
<td>-85</td>
</tr>
<tr>
<td>Jupiter</td>
<td>483.8</td>
<td>-166</td>
</tr>
<tr>
<td>Saturn</td>
<td>890.8</td>
<td>-200</td>
</tr>
<tr>
<td>Uranus</td>
<td>1784.8</td>
<td>-320</td>
</tr>
<tr>
<td>Pluto</td>
<td>3647.2</td>
<td>-375</td>
</tr>
</tbody>
</table>

Source: World Meteorological Association

12. Draw a scatter plot with average distance as the independent variable.

13. Write a prediction equation.

14. Predict the average temperature for Neptune, which has an average distance from the Sun of 2793.1 million miles.

15. Compare your prediction to the actual value of −330°F.

16. **RESEARCH** Use the Internet or other resource to look up the population of your community in several past years. Organize the data as ordered pairs. Then use an equation to predict the population in some future year.

**CHALLENGE** For Exercises 17 and 18, use the table that shows the percent of people ages 25 and over with a high school diploma over the last few decades.

17. Use a prediction equation to predict the percent in 2015.

18. Do you think your prediction is accurate? Explain.
19. **OPEN ENDED** Write a different prediction equation for the data in the example on page 87.

20. **Writing in Math** Use the information on page 86 to explain how a linear equation can model the number of Calories you burn while exercising. Include a scatter plot, a description of the correlation, and a prediction equation for the data. Then predict the number of Calories burned in an hour by a 140-pound person running at 9 miles per hour and compare your predicted value with the actual value of 953.

21. **ACT/SAT** Which line best fits the data in the graph?

![Graph with points and lines]

A. $y = x$
B. $y = -0.5x + 4$
C. $y = -0.5x - 4$
D. $y = 0.5 + 0.5x$

22. **REVIEW** Anna took brownies to a club meeting. She gave half of her brownies to Sarah. Sarah gave a third of her brownies to Rob. Rob gave a fourth of his brownies to Trina. If Trina has 3 brownies, how many brownies did Anna have in the beginning?

- F 12
- G 36
- H 72
- J 144

23. **Spiral Review** Write an equation in slope-intercept form that satisfies each set of conditions. *(Lesson 2-4)*

- 23. slope 4, passes through (0, 6)
- 24. passes through (5, -3) and (-2, 0)

**TELEPHONES** For Exercises 25 and 26, use the following information. *(Lesson 2-4)*

Namid is examining the calling card portion of his phone bill. A 4-minute call at the night rate cost $2.65. A 10-minute call at the night rate cost $4.75.

- 25. Write a linear equation to model this situation.
- 26. How much would it cost to talk for half an hour at the night rate?

Find the slope of the line that passes through each pair of points. *(Lesson 2-3)*

- 27. (5, 4), (-3, 8)
- 28. (-1, -2), (4, -2)
- 29. (3, -4), (3, 16)

30. **PROFIT** Kara is planning to set up a booth at a local festival to sell her paintings. She determines that the amount of profit she will make is determined by the function $P(x) = 11x - 100$, where $x$ is the number of paintings she sells. How much profit will Kara make if she sells 35 of her paintings? *(Lesson 2-1)*

31. **PREREQUISITE SKILL** Find each absolute value. *(Lesson 1-4)*

- 31. $| -3 |$
- 32. $| 11 |$
- 33. $| 0 |$
- 34. $| -\frac{2}{3} |$
- 35. $| -1.5 |$
Graphing Calculator Lab

Lines of Regression

You can use a graphing calculator to find a function that best fits a set of data. The graph of a linear function that models a set of data is called a regression line or line of best fit. You can also use the calculator to draw scatter plots and make predictions.

INCOME The table shows the median income of U.S. families for the period 1970–2002.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Income ($)</td>
<td>9867</td>
<td>21,023</td>
<td>27,735</td>
<td>35,353</td>
<td>40,611</td>
<td>46,737</td>
<td>50,732</td>
<td>51,680</td>
</tr>
</tbody>
</table>

Source: U.S. Census Bureau

Make a scatter plot of the data. Find a function and graph a regression line. Then use the function to predict the median income in 2015.

**STEP 1** Make a scatter plot.
- Enter the years in L1 and the income in L2.
  
  **KEYSTROKES:**
  STAT ENTER 1970
  ENTER 1980 ENTER ...
- Set the viewing window to fit the data.
  **KEYSTROKES:**
  WINDOW 1965 ENTER 2015
  ENTER 5 ENTER 0 ENTER 55000
  ENTER 10000 ENTER
- Use STAT PLOT to graph a scatter plot.
  **KEYSTROKES:**
  2nd [STAT PLOT] ENTER

**STEP 2** Find the equation of a regression line.
- Find the regression equation by selecting LinReg(ax + b) on the STAT CALC menu.
  **KEYSTROKES:**
  STAT 4 ENTER

The regression equation is about \( y = 1349.87x - 2,650,768.34 \). The slope indicates that family incomes were increasing at a rate of about $1350 per year.

The number \( r \) is called the **linear correlation coefficient**. The closer the value of \( r \) is to 1 or -1, the closer the data points are to the line. In this case, \( r \) is very close to 1 so the line fits the data well. If the values of \( r^2 \) and \( r \) are not displayed, use DiagnosticOn from the CATALOG menu.
**EXERCISES**

**BASEBALL**  For Exercises 1–3, use the table at the right that shows the total attendance for minor league baseball in some recent years.

1. Make a scatter plot of the data.
2. Find a regression equation for the data.
3. Predict the attendance in 2010.

<table>
<thead>
<tr>
<th>Year</th>
<th>Attendance (millions)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1985</td>
<td>18.4</td>
</tr>
<tr>
<td>1990</td>
<td>25.2</td>
</tr>
<tr>
<td>1995</td>
<td>33.1</td>
</tr>
<tr>
<td>2000</td>
<td>37.6</td>
</tr>
</tbody>
</table>

Source: National Association of Professional Baseball Leagues

**GOVERNMENT**  For Exercises 4–6, use the table below that shows the population and the number of representatives in Congress for the most populous states.

<table>
<thead>
<tr>
<th>State</th>
<th>CA</th>
<th>TX</th>
<th>NY</th>
<th>FL</th>
<th>IL</th>
<th>PA</th>
<th>OH</th>
</tr>
</thead>
<tbody>
<tr>
<td>Population (millions)</td>
<td>35.5</td>
<td>22.1</td>
<td>19.2</td>
<td>17.0</td>
<td>12.7</td>
<td>12.4</td>
<td>11.4</td>
</tr>
<tr>
<td>Representatives</td>
<td>53</td>
<td>32</td>
<td>29</td>
<td>25</td>
<td>19</td>
<td>19</td>
<td>18</td>
</tr>
</tbody>
</table>

Source: World Almanac

4. Make a scatter plot of the data.
5. Find a regression equation for the data.
6. Predict the number of representatives for South Carolina, which has a population of about 4.1 million.
MUSIC For Exercises 7–11, use the table at the right that shows the percent of music sales that were made in record stores in the United States for the period 1995–2004.

7. Make a scatter plot of the data. Is the correlation of the data positive or negative? Explain.
8. Find a regression equation for the data.
9. According to the regression equation, what was the average rate of change of record store sales during the period?
10. Use the function to predict the percent of sales made in record stores in 2015.
11. How accurate do you think your prediction is? Explain.

RECREATION For Exercises 12–16, use the table at the right that shows the amount of money spent on sporting footwear in some recent years.

12. Find a regression equation for the data.
13. Use the regression equation to predict the sales in 2010.
14. Delete the outlier (1999, 12,546) from the data set and find a new regression equation for the data.
15. Use the new regression equation to predict the sales in 2010.
16. Compare the correlation coefficients for the two regression equations. Which function fits the data better? Which prediction would you expect to be more accurate?

EXTENSION For Exercises 17–20, design and complete your own data analysis.
17. Write a question that could be answered by examining data. For example, you might estimate the number of students who will attend your school 5 years from now or predict the future cost of a piece of electronic equipment.
18. Collect and organize the data you need to answer the question you wrote. You may need to research your topic on the Internet or conduct a survey to collect the data you need.
19. Make a scatter plot and find a regression equation for your data. Then use the regression equation to answer the question.
Main Ideas
- Identify and graph step, constant, and identity functions.
- Identify and graph absolute value and piecewise functions.

Preparation for Standard 1.0
Students solve equations and inequalities involving absolute value. (Key)

New Vocabulary
step function
greatest integer function
constant function
identity function
absolute value function
piecewise function

Study Tip
Greatest Integer Function
Notice that the domain of this step function is all real numbers and the range is all integers.

GET READY for the Lesson
The cost of the postage to mail a letter is a function of the weight of the letter. But the function is not linear. It is a special function called a step function.

For letters with weights between whole numbers, the cost “steps up” to the next higher cost. So the cost to mail a 1.5-ounce letter is the same as the cost to mail a 2-ounce letter, $0.63.

Step Functions, Constant Functions, and the Identity Function
The graph of a step function is not linear. It consists of line segments or rays. The greatest integer function, written \( f(x) = \lfloor x \rfloor \), is an example of a step function. The symbol \( \lfloor x \rfloor \) means the greatest integer less than or equal to \( x \). For example, \( \lfloor 7.3 \rfloor = 7 \) and \( \lfloor -1.5 \rfloor = -2 \) because \( -1 > -1.5 \).

<table>
<thead>
<tr>
<th>( x )</th>
<th>( f(x) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>(-3 \leq x &lt; -2)</td>
<td>(-3)</td>
</tr>
<tr>
<td>(-2 \leq x &lt; -1)</td>
<td>(-2)</td>
</tr>
<tr>
<td>(-1 \leq x &lt; 0)</td>
<td>(-1)</td>
</tr>
<tr>
<td>(0 \leq x &lt; 1)</td>
<td>(0)</td>
</tr>
<tr>
<td>(1 \leq x &lt; 2)</td>
<td>(1)</td>
</tr>
<tr>
<td>(2 \leq x &lt; 3)</td>
<td>(2)</td>
</tr>
<tr>
<td>(3 \leq x \leq 4)</td>
<td>(3)</td>
</tr>
</tbody>
</table>

A dot means that the point is included in the graph.

A circle means that the point is not included in the graph.

Real-World Example
BUSINESS The No Leak Plumbing Repair Company charges $60 per hour or any fraction thereof for labor. Draw a graph that represents this situation.

Explore The total labor charge must be a multiple of $60, so the graph will be the graph of a step function.

Plan If the time spent on labor is greater than 0 hours, but less than or equal to 1 hour, then the labor cost is $60. If the time is greater than 1 hour but less than or equal to 2 hours, then the labor cost is $120, and so on.

(continued on the next page)
Solve  Use the pattern of times and costs to make a table, where $x$ is the number of hours of labor and $C(x)$ is the total labor cost. Then graph.

<table>
<thead>
<tr>
<th>$x$</th>
<th>$C(x)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$0 &lt; x \leq 1$</td>
<td>$60$</td>
</tr>
<tr>
<td>$1 &lt; x \leq 2$</td>
<td>$120$</td>
</tr>
<tr>
<td>$2 &lt; x \leq 3$</td>
<td>$180$</td>
</tr>
<tr>
<td>$3 &lt; x \leq 4$</td>
<td>$240$</td>
</tr>
<tr>
<td>$4 &lt; x \leq 5$</td>
<td>$300$</td>
</tr>
</tbody>
</table>

Check  Since the company rounds any fraction of an hour up to the next whole number, each segment on the graph has a circle at the left endpoint and a dot at the right endpoint.

1. RECYCLING  A recycling company pays $5 for every full box of newspaper. They do not give any money for partial boxes. Draw a graph that shows the amount of money for the number of boxes brought to the center.

You learned in Lesson 2-4 that the slope-intercept form of a linear function is $y = mx + b$, or in function notation, $f(x) = mx + b$.

When $m = 0$, the value of the function is $f(x) = b$ for every $x$-value. So, $f(x) = b$ is called a constant function. The function $f(x) = 0$ is called the zero function.

Another special case of slope-intercept form is $m = 1, b = 0$. This is the function $f(x) = x$. The graph is the line through the origin with slope 1.

Since the function does not change the input value, $f(x) = x$ is called the identity function.

Absolute Value and Piecewise Functions  Another special function is the absolute value function, $f(x) = |x|$.
Lesson 2-6 Special Functions

The absolute value function can be written as \( f(x) = \begin{cases} -x & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases} \). A function that is written using two or more expressions is called a piecewise function. Recall that a family of graphs displays one or more similar characteristics. The parent graph of most absolute value functions is \( y = |x| \).

**EXAMPLE**

**Absolute Value Functions**

Graph \( f(x) = |x| + 1 \) and \( g(x) = |x| - 2 \) on the same coordinate plane.

**THINK AND DISCUSS**

1. What do these graphs have in common?
2. Describe how the graph of \( y = a|x| \) changes as \( a \) increases. Assume \( a > 0 \).
3. Write an absolute value function whose graph is between the graphs of \( y = 2|x| \) and \( y = 3|x| \).
4. Graph \( y = |x| \) and \( y = -|x| \) on the same screen. Then graph \( y = 2|x| \) and \( y = -2|x| \) on the same screen. What is true in each case?
5. In general, what is true about the graph of \( y = a|x| \) when \( a < 0 \)?
To graph other piecewise functions, examine the inequalities in the definition of the function to determine how much of each piece to include.

**EXAMPLE** Piecewise Function

Graph \( f(x) = \begin{cases} x - 4 & \text{if } x < 2 \\ 1 & \text{if } x \geq 2 \end{cases} \)

**Step 1** Graph the linear function \( f(x) = x - 4 \) for \( x < 2 \).
Since 2 does not satisfy this inequality, stop with an open circle at \((2, -2)\).

**Step 2** Graph the constant function \( f(x) = 1 \) for \( x \geq 2 \).
Since 2 does satisfy this inequality, begin with a closed circle at \((2, 1)\) and draw a horizontal ray to the right.

The function is defined for all values of \( x \), so the domain is all real numbers. The values that are \( y \)-coordinates of points on the graph are 1 and all real numbers less than \(-2\), so the range is \( \{ y | y < -2 \text{ or } y = 1 \} \).

Check Your Progress

3. Graph \( f(x) = \begin{cases} x + 2 & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases} \)
Identify the domain and range.

**CONCEPT SUMMARY**

<table>
<thead>
<tr>
<th>Step Function</th>
<th>Constant Function</th>
<th>Absolute Value Function</th>
<th>Piecewise Function</th>
</tr>
</thead>
<tbody>
<tr>
<td>horizontal segments and/or rays</td>
<td>horizontal line</td>
<td>V-shape</td>
<td>different rays, segments, and curves</td>
</tr>
</tbody>
</table>

**EXAMPLE** Identify Functions

Determine whether each graph represents a step function, a constant function, an absolute value function, or a piecewise function.

a. The graph has multiple horizontal segments. It represents a step function.

b. The graph is a horizontal line. It represents a constant function.
Graph each function. Identify the domain and range.

1. \( f(x) = -[x] \)  
2. \( g(x) = [2x] \)  
3. \( f(x) = 4 \)  
4. \( z(x) = -3 \)  
5. \( h(x) = |x| - 3 \)  
6. \( f(x) = |3x - 2| \)  
7. \( g(x) = \begin{cases} 
-1 & \text{if } x < 0 \\
-x + 2 & \text{if } x \geq 0 
\end{cases} \)  
8. \( h(x) = \begin{cases} 
2x & \text{if } x > -1 \\
0 & \text{if } x \leq -1 
\end{cases} \)

Identify each function as S for step, C for constant, A for absolute value, or P for piecewise.

9. \( f(x) = \begin{cases} 
2 & \text{if } x < 3 \\
1 & \text{if } x \geq 3 
\end{cases} \)

Parking For Exercises 11–13, use the following information.
A downtown parking lot charges $2 for the first hour and $1 for each additional hour or part of an hour.

11. What type of special function models this situation?
12. Draw a graph of a function that represents this situation.
13. Use the graph to find the cost of parking there for \( \frac{11}{2} \) hours.

Graph each function. Identify the domain and range.

14. \( f(x) = [x + 3] \)  
15. \( g(x) = [x - 2] \)  
16. \( f(x) = 2[x] \)  
17. \( h(x) = -3[x] \)  
18. \( g(x) = [x] + 3 \)  
19. \( f(x) = [x] - 1 \)  
20. \( f(x) = |2x| \)  
21. \( h(x) = |-x| \)  
22. \( g(x) = |x| + 3 \)  
23. \( g(x) = |x| - 4 \)  
24. \( h(x) = |x + 3| \)  
25. \( f(x) = |x + 2| \)  
26. \( f(x) = \begin{cases} 
-x & \text{if } x \leq 3 \\
2 & \text{if } x > 3 
\end{cases} \)  
27. \( h(x) = \begin{cases} 
-1 & \text{if } x < -2 \\
1 & \text{if } x > 2 
\end{cases} \)
Identify each function as S for step, C for constant, A for absolute value, or P for piecewise.

28. $f(x) = \begin{cases} \frac{x}{4} & \text{if } x < -3 \\ 2 & \text{if } -3 \leq x < 1 \\ -2x + 2 & \text{if } x \geq 1 \end{cases}$

29. $f(x) = \begin{cases} x - \frac{1}{4} & \text{if } x \leq -3 \\ \frac{x}{2} & \text{if } -3 < x < 1 \\ -x + 1 & \text{if } x \geq 1 \end{cases}$

30. $f(x) = \begin{cases} x & \text{if } x \leq -3 \\ \frac{x}{2} & \text{if } -3 < x < 1 \\ -x + 1 & \text{if } x \geq 1 \end{cases}$

31. $f(x) = \begin{cases} x & \text{if } x \leq -3 \\ \frac{x}{2} & \text{if } -3 < x < 1 \\ -x + 1 & \text{if } x \geq 1 \end{cases}$

32. $f(x) = \begin{cases} x & \text{if } x \leq -3 \\ \frac{x}{2} & \text{if } -3 < x < 1 \\ -x + 1 & \text{if } x \geq 1 \end{cases}$

33. $f(x) = \begin{cases} x & \text{if } x \leq -3 \\ \frac{x}{2} & \text{if } -3 < x < 1 \\ -x + 1 & \text{if } x \geq 1 \end{cases}$

34. **THEATER** Springfield High School’s theater can hold 250 students. The drama club is performing a play in the theater. Draw a graph of a step function that shows the relationship between the number of tickets sold $x$ and the minimum number of performances $y$ that the drama club must do.

Graph each function. Identify the domain and range.

35. $f(x) = \left| x - \frac{1}{4} \right|$  

36. $f(x) = \left| x + \frac{1}{2} \right|$  

37. $f(x) = \begin{cases} x & \text{if } x < -3 \\ 2 & \text{if } -3 \leq x < 1 \\ -2x + 2 & \text{if } x \geq 1 \end{cases}$  

38. $g(x) = \begin{cases} -1 & \text{if } x \leq -2 \\ x & \text{if } -2 < x < 2 \\ -x + 1 & \text{if } x \geq 2 \end{cases}$  

39. $f(x) = \left[ \left\lfloor |x| \right\rfloor \right]$  

40. $g(x) = \left\lfloor |x| \right\rfloor$

**TELEPHONE RATES** For Exercises 41 and 42, use the following information. Masao has a long-distance telephone plan where she pays 10¢ for each minute or part of a minute that she talks, regardless of the time of day.

41. Graph a step function that represents this situation.

42. How much would a call that lasts 9 minutes and 40 seconds cost?

**NUTRITION** For Exercises 43–45, use the following information. The recommended dietary allowance for vitamin C is 2 micrograms per day.

43. Write an absolute value function for the difference between the number of micrograms of vitamin C you ate today $x$ and the recommended amount.

44. What is an appropriate domain for the function?

45. Use the domain to graph the function.

46. **INSURANCE** According to the terms of Lavon’s insurance plan, he must pay the first $300 of his annual medical expenses. The insurance company pays 80% of the rest of his medical expenses. Write a function for how much the insurance company pays if $x$ represents Lavon’s annual medical expenses.

47. **OPEN ENDED** Write a function involving absolute value for which $f(-2) = 3$.

48. **REASONING** Find a counterexample to the statement *To find the greatest integer function of $x$ when $x$ is not an integer, round $x$ to the nearest integer.*

49. **CHALLENGE** Graph $|x| + |y| = 3$. 

---

**Real-World Link**

Good sources of vitamin C include citrus fruits and juices, cantaloupe, broccoli, Brussels sprouts, potatoes, sweet potatoes, tomatoes, and cabbage.

Source: *The World Almanac*
50. Writing in Math Use the information on page 95 to explain how step functions apply to postage rates. Explain why a step function is the best model for this situation while your gas mileage as a function of time as you drive to the post office cannot be modeled with a step function. Then graph the function that represents the cost of a first-class letter.

51. ACT/SAT For which function does 
   \( f\left(-\frac{1}{2}\right) \neq -1? \)
   A  \( f(x) = 2x \)  
   B  \( f(x) = \left|-2x\right| \)  
   C  \( f(x) = \left[x\right] \)  
   D  \( f(x) = \left[2x\right] \)

52. ACT/SAT For which function is the range \( \{y \mid y \leq 0\} \)?
   F  \( f(x) = -x \)  
   G  \( f(x) = \left[x\right] \)  
   H  \( f(x) = \left|x\right| \)  
   J  \( f(x) = \left|-x\right| \)

53. REVIEW Solve: \( 5(x + 4) = x + 4 \)
   Step 1: \( 5x + 20 = x + 4 \)
   Step 2: \( 4x + 20 = 4 \)
   Step 3: \( 4x = 24 \)
   Step 4: \( x = 6 \)
   Which is the first incorrect step in the solution shown above?
   A  Step 4  
   B  Step 3  
   C  Step 2  
   D  Step 1

HEALTH For Exercises 54–56, use the table that shows the life expectancy for people born in various years. (Lesson 2-5)

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Expectancy</td>
<td>68.2</td>
<td>69.7</td>
<td>70.8</td>
<td>73.7</td>
<td>75.4</td>
<td>77.0</td>
</tr>
</tbody>
</table>

Source: National Center for Health Statistics

54. Draw a scatter plot in which \( x \) is the number of years since 1940 and describe the correlation.
55. Find a prediction equation.
56. Predict the life expectancy of a person born in 2010.

Write an equation in slope-intercept form that satisfies each set of conditions. (Lesson 2-4)

57. slope 3, passes through \((-2, 4)\)  
58. passes through \((0, -2)\) and \((4, 2)\)

Solve each inequality. Graph the solution set. (Lesson 1-3)

59. \( 3x - 5 \geq 4 \)  
60. \( 28 - 6y < 23 \)

PREREQUISITE SKILL Determine whether \((0, 0)\) satisfies each inequality. Write yes or no. (Lesson 1-5)

61. \( y < 2x + 3 \)  
62. \( y \geq -x + 1 \)  
63. \( y \leq \frac{3}{4}x - 5 \)  
64. \( 2x + 6y + 3 > 0 \)  
65. \( y > |x| \)  
66. \( |x| + y \leq 3 \)
Main Ideas
- Graph linear inequalities.
- Graph absolute value inequalities.

Graph Linear Inequalities A linear inequality resembles a linear equation, but with an inequality symbol instead of an equals symbol. For example, \( y \leq 2x + 1 \) is a linear inequality and \( y = 2x + 1 \) is the related linear equation.

The graph of the inequality \( y \leq 2x + 1 \) is the shaded region. Every point in the shaded region satisfies the inequality. The graph of \( y = 2x + 1 \) is the boundary of the region. It is drawn as a solid line to show that points on the line satisfy the inequality. If the inequality symbol were < or >, then points on the boundary would not satisfy the inequality, so the boundary would be drawn as a dashed line.

**EXAMPLE** Dashed Boundary

Graph \( 2x + 3y > 6 \).

The boundary is the graph of \( 2x + 3y = 6 \). Since the inequality symbol is >, the boundary will be dashed.

Now test the point \((0, 0)\).

\[
2x + 3y > 6 \quad \text{Original inequality} \\
2(0) + 3(0) > 6 \quad (x, y) = (0, 0) \\
0 > 6 \quad \text{false}
\]

Shade the region that does not contain \((0, 0)\).

**CHECK Your Progress**

1A. Graph \( 3x + \frac{1}{2}y < 2 \).

1B. Graph \( -x + 2y > 4 \).
**BUSINESS** A mail-order company is hiring temporary employees to help in its packing and shipping departments during their peak season.

a. Write and graph an inequality to describe the number of employees that can be assigned to each department if the company has 20 temporary employees available.

Let \( p \) be the number of employees assigned to packing and let \( s \) be the number assigned to shipping. Since the company can assign at most 20 employees total to the two departments, use a \( \leq \) symbol.

The employees are at most twenty.

\[
p + s \leq 20
\]

Since the inequality symbol is \( \leq \), the graph of the related linear equation \( p + s = 20 \) is solid.

Test \((0, 0)\).

\[
\begin{align*}
p + s &\leq 20 \quad \text{Original inequality} \\
0 + 0 &\leq 20 \quad (p, s) = (0, 0) \\
0 &\leq 20 \quad \text{true}
\end{align*}
\]

Shade the region that contains \((0, 0)\). Since the variables cannot be negative, shade only the part in the first quadrant.

b. Can the company assign 8 employees to packing and 10 to shipping?

The point \((8, 10)\) is in the shaded region, so it satisfies the inequality. The company can assign 8 employees to packing and 10 to shipping.

---

**Graph Absolute Value Inequalities** Graphing absolute value inequalities is similar to graphing linear inequalities.

**EXAMPLE**

Graph \( y < |x| + 1 \).

Since the inequality symbol is \(<\), the boundary is dashed. Graph the equation. Then test \((0, 0)\).

\[
y < |x| + 1 \quad \text{Original inequality} \\
0 < |0| + 1 \quad (x, y) = (0, 0) \\
0 < 0 + 1 \quad |0| = 0 \\
0 < 1 \quad \text{true}
\]

Shade the region that includes \((0, 0)\).

3. Graph \( y > 2|x| - 3 \).
Homework

For Exercises 10–15
See Examples 1
For Exercises 16–19, 22–26
See Examples 2
For Exercises 20–21
See Examples 3

Real-World Link

A dividend is a payment from a company to an investor. It is a way to make money on a stock without selling it.

Graph each inequality.
1. \( y < 2 \)
2. \( y > 2x - 3 \)
3. \( x - y \geq 0 \)
4. \( x - 2y \leq 5 \)
5. \( y > |2x| \)
6. \( y \leq 3|x| - 1 \)

Shopping

For Exercises 7–9, use the following information.
Gwen wants to buy some used CDs that cost $10 each and some used DVDs that cost $13 each. She has $40 to spend.
7. Write an inequality to represent the situation, where \( c \) is the number of CDs she buys and \( d \) is the number of DVDs.
8. Graph the inequality.
9. Can she buy 2 CDs and 3 DVDs? Explain.

Finance

For Exercises 24–26, use the following information.
Carl Talbert estimates that he will need to earn at least $9000 per year combined in dividend income from the two stocks he owns to supplement his retirement plan.
24. Write an inequality to represent this situation.
25. Graph the inequality.
26. Will he make enough from 3000 shares of each company?

Graph each inequality.
29. \( 4x - 5y - 10 \leq 0 \)
30. \( y \geq \frac{1}{2}x - 5 \)
31. \( y + |x| < 3 \)
32. \( y \geq |x - 1| - 2 \)
33. \( |x + y| > 1 \)
34. \( |x| \leq |y| \)

Help

Examples 1–3 (pp. 102–103)

Example 2 (p. 103)
Graphing Inequalities

SHADE( COMMAND You can graph inequalities by using the SHADE( command located in the DRAW menu. Enter two functions.
- The first function defines the lower boundary of the shaded region. If the inequality is “$, use the Ymin window value as the lower boundary.
- The second function defines the upper boundary of the region. If the inequality is “$, use the Ymax window value as the upper boundary.

Graph each inequality.
35. \( y \geq 3 \)
36. \( y \leq x + 2 \)
37. \( y \leq -2x - 4 \)
38. \( x - 7 \leq y \)
39. REASONING Explain how to determine which region to shade when graphing an inequality.
40. CHALLENGE Graph \( |y| < x \).
41. Writing in Math Use the information on page 102 to write an inequality that defines a good game for Drew Brees in Dana’s fantasy football league, and explain how you obtained it.

**STANDARDS PRACTICE**

42. ACT/SAT Which could be the inequality for the graph?
   A. \( y < 3x + 2 \)
   B. \( y \leq 3x + 2 \)
   C. \( y > 3x + 2 \)
   D. \( y \geq 3x + 2 \)

43. REVIEW What is the solution set of the inequality?
   \( 6 - |x + 7| \leq -2 \)
   F. \( -15 \leq x + 1 \)
   G. \( -1 \leq x \leq 3 \)
   H. \( x \leq -1 \) or \( x \geq 3 \)
   J. \( x \leq -15 \) or \( x \geq 1 \)

**SPIRAL REVIEW**

Graph each function. Identify the domain and range. (Lesson 2-6)
44. \( f(x) = \lfloor x \rfloor - 4 \)
45. \( g(x) = |x| - 1 \)
46. \( h(x) = |x - 3| \)

SALARY For Exercises 47–49, use the table which shows the years of experience for eight computer programmers and their yearly salary. (Lesson 2-5)

<table>
<thead>
<tr>
<th>Years</th>
<th>6</th>
<th>5</th>
<th>3</th>
<th>1</th>
<th>4</th>
<th>3</th>
<th>6</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Salary ($)</td>
<td>55,000</td>
<td>53,000</td>
<td>45,000</td>
<td>42,000</td>
<td>48,500</td>
<td>46,500</td>
<td>53,000</td>
<td>43,000</td>
</tr>
</tbody>
</table>

47. Draw a scatter plot and describe the correlation.
48. Find a prediction equation.
49. Predict the salary for a representative with 9 years of experience.

Solve each equation. Check your solution. (Lesson 1-3)
50. \( 4x - 9 = 23 \)
51. \( 11 - 2y = 5 \)
52. \( 2z - 3 = -6z + 1 \)
Chapter 2
Linear Relations and Functions

Study Guide
and Review

Vocabulary Check

Key Concepts

Relations and Functions (Lesson 2-1)
- A relation is a set of ordered pairs. The domain is the set of all x-coordinates, and the range is the set of all y-coordinates.
- A function is a relation where each member of the domain is paired with exactly one member of the range.

Linear Equations and Slope (Lessons 2-2 to 2-4)
- A linear equation is an equation whose graph is a line.
- Slope is the ratio of the change in y-coordinates to the corresponding change in x-coordinates.
- Lines with the same slope are parallel. Lines with slopes that are opposite reciprocals are perpendicular.
- Standard Form: $Ax + By = C$, where $A$, $B$, and $C$ are integers whose greatest common factor is 1, $A \geq 0$, and $A$ and $B$ are not both zero
- Slope-Intercept Form: $y = mx + b$
- Point-Slope Form: $y - y_1 = m(x - x_1)$

Using Scatter Plots (Lesson 2-5)
- A prediction equation can be used to predict the value of one of the variables given the value of the other variable.

Graphing Inequalities (Lesson 2-7)
- You can graph an inequality by following these steps.
  Step 1: Determine whether the boundary is solid or dashed. Graph the boundary.
  Step 2: Choose a point not on the boundary and test it in the inequality.
  Step 3: If a true inequality results, shade the region containing your test point. If a false inequality results, shade the other region.

Key Vocabulary

absolute value function (p. 96)
boundary (p. 102)
constant function (p. 96)
continuous function (p. 65)
coordinate plane (p. 58)
dependent variable (p. 61)
discrete function (p. 65)
domain (p. 58)
family of graphs (p. 73)
function (p. 58)
function notation (p. 61)
greatest integer function (p. 95)
identity function (p. 96)
independent variable (p. 61)
linear equation (p. 66)
linear function (p. 66)
line of fit (p. 86)
mapping (p. 58)
negative correlation (p. 86)
no correlation (p. 86)
one-to-one function (p. 58)
ordered pair (p. 58)
parent graph (p. 73)
piecewise function (p. 97)
point-slope form (p. 80)
prediction equation (p. 86)
quadrant (p. 58)
range (p. 58)
rate of change (p. 71)
relation (p. 58)
scatter plot (p. 86)
slope (p. 71)
slope-intercept form (p. 79)
standard form (p. 67)
step function (p. 95)
vertical line test (p. 59)
x-intercept (p. 68)

Vocabulary Review at ca.algebra2.com
Lesson-by-Lesson Review

2–1 Relations and Functions (pp. 58–64)

Graph each relation or equation and find the domain and range. Then determine whether the relation or equation is a function. Is the relation discrete or continuous?

7. \{(6, 3), (2, 1), (−2, 3)\}
8. \{(-5, 2), (2, 4), (1, 1), (−5, −2)\}
9. \(y = 0.5x\)
10. \(y = 2x + 1\)

Find each value if \(f(x) = 5x - 9\).

11. \(f(6)\)
12. \(f(-2)\)
13. \(f(y)\)
14. \(f(-2v)\)

15. **TAXI RIDE** A taxi company charges $2.80 for the first mile and $1.60 for each additional mile. The amount a passenger will be charged can be expressed as \(f(x) = 1.20 + 1.60x\), when \(x \geq 1\). Graph this equation and find the domain and range. Then determine whether the equation is a function. Is the equation discrete or continuous?

Example 1 Graph the relation \{(-3, 1), (0, 2), (2, 5)\} and find the domain and range. Then determine whether the relation is a function. Is the relation discrete or continuous?

The domain is \{-3, 0, 2\}, and the range is \{1, 2, 5\}.

Since each \(x\)-value is paired with exactly one \(y\)-value, the relation is a function. The relation is discrete because the points are not connected.

Example 2 Write \(2x - 6 = y + 8\) in standard form. Identify \(A, B,\) and \(C\).

\[
\begin{align*}
2x &- 6 = y + 8 & \text{Original equation} \\
2x &- y = 6 & \text{Subtract } y \text{ from each side.} \\
2x &- y = 14 & \text{Add 6 to each side.}
\end{align*}
\]

The standard form is \(2x - y = 14\). So, \(A = 2, B = -1,\) and \(C = 14\).

2–2 Linear Equations (pp. 66–70)

State whether each equation or function is linear. Write yes or no. If no, explain your reasoning.

16. \(2x + y = 11\)
17. \(h(x) = \sqrt{2x + 1}\)

Write each equation in standard form. Identify \(A, B,\) and \(C\).

18. \(\frac{2}{3}x - \frac{3}{4}y = 6\)
19. \(0.5x = -0.2y - 0.4\)

Find the \(x\)-intercept and the \(y\)-intercept of the graph of each equation. Then graph the equation.

20. \(-\frac{1}{5}y = x + 4\)
21. \(6x = -12y + 48\)

22. **CUBES** Julián thinks that the equation for the volume of a cube, \(V = s^3\), is a linear equation. Is he correct? Explain.
Slope (pp. 71–77)

Find the slope of the line that passes through each pair of points.
23. \((-6, -3), (6, 7)\)  
24. \((5.5, -5.5), (11, -7)\)

Graph the line passing through the given point with the given slope.
25. \((0, 1), m = 2\)  
26. \((-5, 2), m = \frac{-1}{4}\)

Graph the line that satisfies each set of conditions.
27. passes through \((-1, -2)\), perpendicular to a line whose slope is \(\frac{1}{2}\)
28. passes through \((-1, 2)\), parallel to the graph of \(x - 3y = 14\)
29. Ramps  Jack measures his bicycle ramp and finds that it is 5 feet long and 3 feet high. What is the slope of his ramp?

Example 3  Graph the line passing through \((3, 4)\) with slope \(m = \frac{1}{3}\).
Graph the ordered pair \((3, 4)\). Then, according to the slope, go up 1 unit and right 3 units. Plot the new point at \((6, 5)\). You can also go right 3 units and then up 1 unit to plot the new point.

Draw the line containing the points.

Example 4  Write an equation in slope-intercept form for the line through \((4, 5)\) that is parallel to the line through \((-1, -3)\) and \((2, -1)\).
First, find the slope of the given line.
\[
m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - (-3)}{2 - (-1)} = \frac{2}{3}
\]
The parallel line will also have a slope of \(\frac{2}{3}\).  
\[
y - y_1 = m(x - x_1) \\
y - 5 = \frac{2}{3}(x - 4) \\
y = \frac{2}{3}x + \frac{7}{3}
\]

Writing Linear Equations (pp. 79–84)

Write an equation in slope-intercept form for the line that satisfies each set of conditions.
30. slope \(\frac{3}{4}\) passes through \((-6, 9)\)
31. passes through \((-1, 2)\), parallel to the graph of \(x - 3y = 14\)
32. passes through \((3, -8)\) and \((-3, 2)\)
33. passes through \((3, 2)\), perpendicular to the graph of \(4x - 3y = 12\)
34. Landscaping  Mr. Ryan is planning to plant rows of roses in a garden he is designing for a client. Before planting, he sketches out his plans on a coordinate grid. A row of white roses will be planted along the line with equation \(y = 2x + 1\). A row of red roses will be parallel to the white roses and pass through the point \((3, 5)\). What equation would represent the line for the row of red roses?
Chapter 2  Study Guide and Review

Statistics: Using Scatter Plots (pp. 86–91)

**HEALTH INSURANCE** For Exercises 35 and 36 use the table that shows the number of people covered by private or government health insurance in the United States.

<table>
<thead>
<tr>
<th>Year</th>
<th>People (millions)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1988</td>
<td>211</td>
</tr>
<tr>
<td>1992</td>
<td>218</td>
</tr>
<tr>
<td>1996</td>
<td>225</td>
</tr>
<tr>
<td>2000</td>
<td>240</td>
</tr>
<tr>
<td>2004</td>
<td>245</td>
</tr>
</tbody>
</table>

Source: U.S. Census

35. Draw a scatter plot and describe the correlation.

36. Use two ordered pairs to write a prediction equation. Then use your prediction equation to predict the number of people with health insurance in 2010.

**GOLD PRODUCTION** For Exercises 37 and 38, use the table that shows the number of ounces of gold produced in the United States for several years.

<table>
<thead>
<tr>
<th>Year</th>
<th>Troy ounces (millions)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1998</td>
<td>11.8</td>
</tr>
<tr>
<td>1999</td>
<td>11.0</td>
</tr>
<tr>
<td>2000</td>
<td>11.3</td>
</tr>
<tr>
<td>2001</td>
<td>10.8</td>
</tr>
<tr>
<td>2002</td>
<td>9.6</td>
</tr>
<tr>
<td>2003</td>
<td>8.9</td>
</tr>
</tbody>
</table>

Source: World Almanac

37. Draw a scatter plot and describe the correlation.

38. Use two ordered pairs to write a prediction equation. Then use your prediction equation to predict the number of ounces of gold that will be produced in 2010.

Example 5 **WEEKLY PAY** The table below shows the median weekly earnings for American workers for the period 1985–1999. Predict the median weekly earnings for 2010.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Earnings ($)</td>
<td>484</td>
<td>541</td>
<td>605</td>
<td>647</td>
<td>?</td>
</tr>
</tbody>
</table>

Source: U.S. Bureau of Labor Statistics

Median Weekly Earnings

Use (1995, 484) and (2004, 647) to find a prediction equation.

\[
m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Slope formula}
\]

\[
= \frac{647 - 484}{2004 - 1995} = \frac{163}{9} \approx 18.1 \quad \text{Simplify.}
\]

\[
y - y_1 = m(x - x_1) \quad \text{Point-slope form}
\]

\[
y - 484 = 18.1(x - 1995) \quad \text{Substitute.}
\]

\[
y - 484 = 18.1x - 36,109.5 \quad \text{Multiply.}
\]

\[
y = 18.1x - 35,625.5 \quad \text{Add 484 to each side.}
\]

To predict earnings for 2010, substitute 2010 for \(x\).

\[
y = 18.1(2010) - 35,625.5 \quad x = 2010
\]

\[
y = 755.5 \quad \text{Simplify.}
\]

The model predicts median weekly earnings of $755.50 in 2010.
**Study Guide and Review**

**2–6**  
**Special Functions** (pp. 95–101)  
Graph each function. Identify the domain and range.  
39. \( f(x) = \lfloor x \rfloor - 2 \)  
40. \( h(x) = \lfloor 2x - 1 \rfloor \)  
41. \( g(x) = |x| + 4 \)  
42. \( h(x) = |x - 1| - 7 \)  
43. \( f(x) = \begin{cases} 
2 & \text{if } x < -1 \\
-x - 1 & \text{if } x \geq -1 
\end{cases} \)  
44. \( g(x) = \begin{cases} 
-2x - 3 & \text{if } x < 1 \\
x - 4 & \text{if } x \geq 1 
\end{cases} \)  
45. **WIRELESS INTERNET** A wireless Internet provider charges $40 a month plus an additional 30 cents a minute or any fraction thereof. Draw a graph that represents this situation.

**Example 6** Graph the function \( f(x) = 3\lfloor x \rfloor - 2 \). Identify the domain and range.  

The domain is all real numbers. The range is all real numbers greater than or equal to \(-2\).

**2–7**  
**Graphing Inequalities** (pp. 102–105)  
Graph each inequality.  
46. \( y \leq 3x - 5 \)  
47. \( x > y - 1 \)  
48. \( y + 0.5x < 4 \)  
49. \( 2x + y \geq 3 \)  
50. \( y \geq |x| + 2 \)  
51. \( y > |x - 3| \)  
52. **BASEBALL** The Cincinnati Reds must score more runs than their opponent to win a game. Write an inequality to represent this situation. Graph the inequality.

**Example 7** Graph \( x + 4y \leq 4 \).  
Since the inequality symbol is \( \leq \), the graph of the boundary should be solid. Graph the equation.  
Test \((0, 0)\).  
\[ x + 4y \leq 4 \quad \text{Original inequality} \]  
\[ 0 + 4(0) \leq 4 \quad (x, y) = (0, 0) \]  
\[ 0 \leq 4 \quad \text{Shade the region that contains } (0, 0) \]
Graph each relation and find the domain and range. Then determine whether the relation is a function.

1. \{(-4, -8), (-2, 2), (0, 5), (2, 3), (4, -9)\}
2. \(y = 3x - 3\)

Find each value.

3. \(f(3)\) if \(f(x) = 7 - x^2\)
4. \(f(0)\) if \(f(x) = x - 3x^2\)

Graph each equation or inequality.

5. \(y = \frac{3}{5}x - 4\)
6. \(4x - y = 2\)
7. \(x = -4\)
8. \(y = 2x - 5\)
9. \(f(x) = 3x - 1\)
10. \(f(x) = |3x| + 3\)
11. \(g(x) = |x + 2|\)
12. \(y \leq 10\)
13. \(-2x + 5 \leq 3y\)
14. \(y < 4|x - 1|\)
15. \(h(x) = \begin{cases} x + 2 & \text{if } x < -2 \\ 2x - 1 & \text{if } x \geq -2 \end{cases}\)

Find the slope of the line that passes through each pair of points.

16. \((6, 1), (8, -4)\)
17. \((-2, 5), (4, 5)\)

Graph the line passing through the given point with the given slope.

20. \((1, -3), \frac{2}{3}\)
21. \((-2, 2), -\frac{1}{3}\)
22. \((3, -2), \text{undefined}\)

Write an equation in slope-intercept form for the line that satisfies each set of conditions.

23. slope \(-5, y\)-intercept 11
24. \(x\)-intercept 9, \(y\)-intercept \(-4\)
25. passes through \((-6, 15)\), parallel to the graph of \(2x + 3y = 1\)
26. passes through \((5, 2)\), perpendicular to the graph of \(x + 3y = 7\)

**RECREATION** For Exercises 27–29, use the table that shows the amount Americans spent on admission to spectator amusements in some recent years.

<table>
<thead>
<tr>
<th>Year</th>
<th>Amount (billion $)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2000</td>
<td>30.4</td>
</tr>
<tr>
<td>2001</td>
<td>32.2</td>
</tr>
<tr>
<td>2002</td>
<td>34.6</td>
</tr>
<tr>
<td>2003</td>
<td>35.6</td>
</tr>
</tbody>
</table>

Source: Bureau of Economic Analysis, U.S. Dept. of Commerce

27. Draw a scatter plot. Let \(x\) represents the number of years since 2000.
28. Write a prediction equation.
29. Predict the amount that will be spent on recreation in 2015.

30. **MULTIPLE CHOICE** What is the slope of a line parallel to \(y - 2 = 4(x + 1)\)?
   A. \(-4\)
   B. \(-\frac{1}{4}\)
   C. \(\frac{1}{4}\)
   D. 4
Red each question. Then fill in the correct answer on the answer document provided by your teacher or on a sheet of paper.

1. Given the function \( y = 2.24x + 16.45 \), which statement best describes the effect of moving the graph down two units?
   A. The \( x \)-intercept decreases.
   B. The \( y \)-intercept decreases.
   C. The \( x \)-intercept remains the same.
   D. The \( y \)-intercept remains the same.

2. Maelea sells engraved necklaces over the Internet. She purchases 50 necklaces for \( \$400 \), and it costs her an additional \( \$3 \) for each personalized engraving. If she charges \( \$20 \) each, how many necklaces will she need to sell in order to make a profit of at least \( \$225 \)?

3. Which equation is represented in the graph below?

4. What is the slope of the line that is parallel to the graph of \( y = 2x + 3 \) and passes through the point \((0, -4)\)?

5. Which graph best represents all the pairs of numbers \((x, y)\), such that \( x - y > 2 \)?

6. Solve \(|2x - 5| = 17\).
   F. \(-6, -11\)
   G. \(-6, 11\)
   H. \(6, -11\)
   J. \(6, 11\)

7. Simplify \(4(x - 5) + 6x \cdot 3 + 8\).
   A. \(22x - 12\)
   B. \(22x + 12\)
   C. \(2x - 9\)
   D. \(2x + 9\)

---

**Question 7** On multiple choice questions, try to compute the answer first. Then compare your answer to the given answer choices. If you don’t find your answer among the choices, check your calculations.
8. Use the table to determine the expression that best represents the sum of the degree measures of the interior angles of a polygon with \( n \) sides.

<table>
<thead>
<tr>
<th>Polygon</th>
<th>Number of Sides</th>
<th>Sum of Measures</th>
</tr>
</thead>
<tbody>
<tr>
<td>Triangle</td>
<td>3</td>
<td>180</td>
</tr>
<tr>
<td>Quadrilateral</td>
<td>4</td>
<td>360</td>
</tr>
<tr>
<td>Pentagon</td>
<td>5</td>
<td>540</td>
</tr>
<tr>
<td>Hexagon</td>
<td>6</td>
<td>720</td>
</tr>
<tr>
<td>Heptagon</td>
<td>7</td>
<td>900</td>
</tr>
<tr>
<td>Octagon</td>
<td>8</td>
<td>1080</td>
</tr>
</tbody>
</table>

\[ F \ 60n \quad H \ 180 + n \quad G \ 180n \quad J \ 180(n - 2) \]

9. GEOMETRY Which of the following are congruent?

A. \( A \cong B \)
B. \( A \cong D \)
C. \( B \cong C \)
D. \( C \cong D \)

10. Rich’s Pet Store sells cat food. The cost of two 5-pound bags is $7.99. The total cost \( c \) of purchasing \( n \) bags can be found by—
   F. multiplying \( n \) by \( c \).
   G. multiplying \( n \) by 5.
   H. multiplying \( n \) by the cost of 1 bag.
   J. dividing \( n \) by \( c \).

Pre-AP/Anchor Problem

11. Stephen owns an electronics store and also has a Web site to sell his products. He has a delivery van for local deliveries and uses a commercial shipper for long-distance deliveries. It costs $0.37 per mile for his local delivery truck. The commercial shipper uses the rates in the table below.

<table>
<thead>
<tr>
<th>Electronic Shipping Charges</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weight (lb)</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>3</td>
</tr>
<tr>
<td>7</td>
</tr>
<tr>
<td>10</td>
</tr>
<tr>
<td>15</td>
</tr>
</tbody>
</table>

a. Write an equation for the cost of shipping using the commercial shipper \( c \) as a function of weight \( p \).

b. Would it be less expensive for Stephen to use his delivery truck or commercially ship a package weighing 13 pounds to a destination that is 30 miles away?